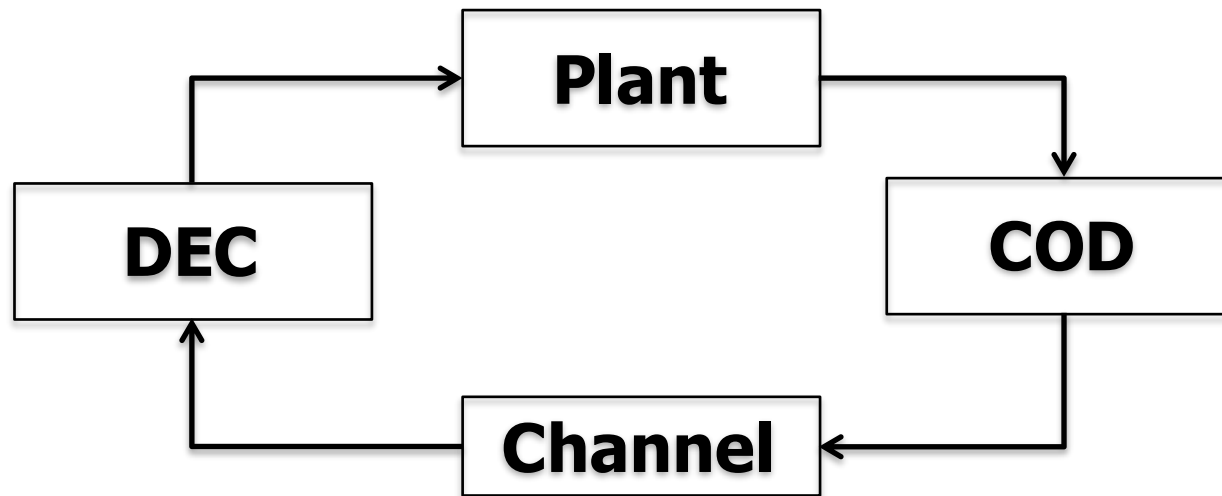


# Control over wireless: an unfinished journey



**Luca Schenato**

University of Padova

Online Seminar on Control and Information

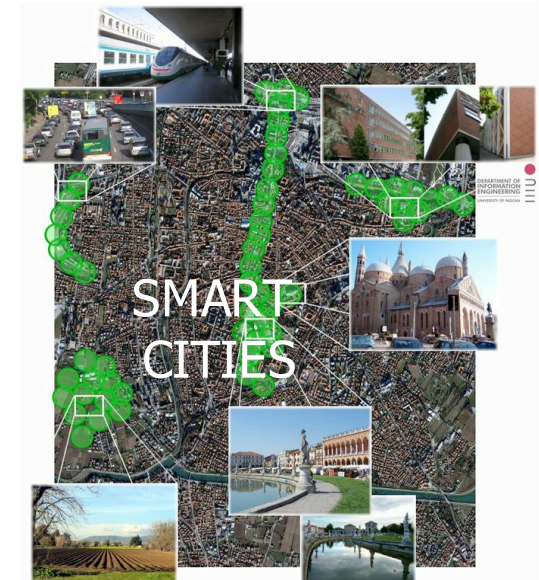
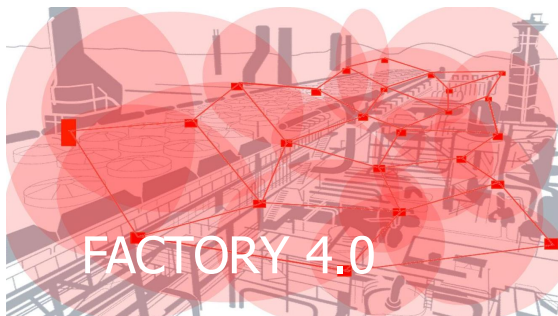
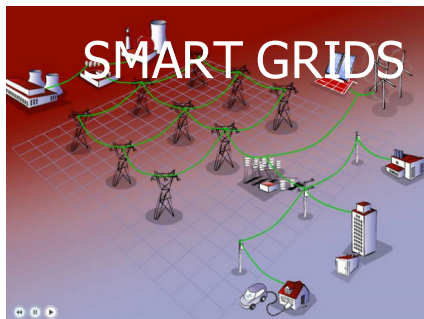
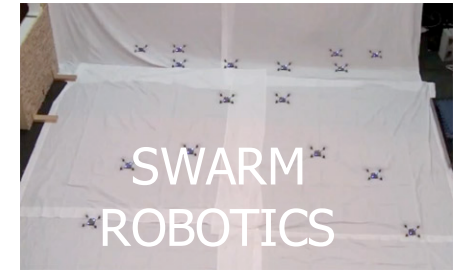
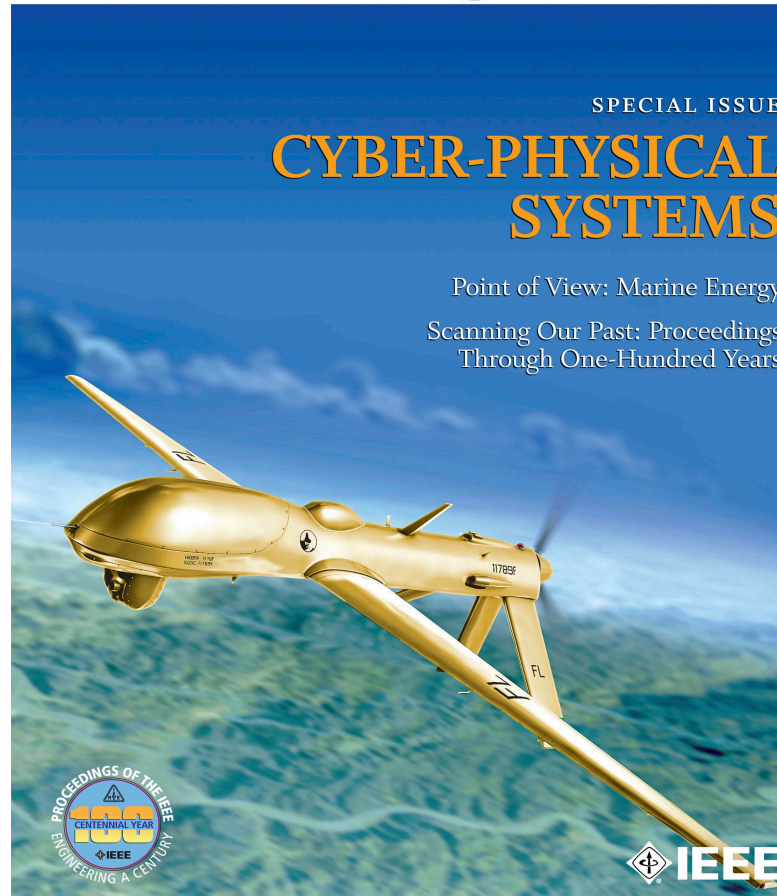
2021



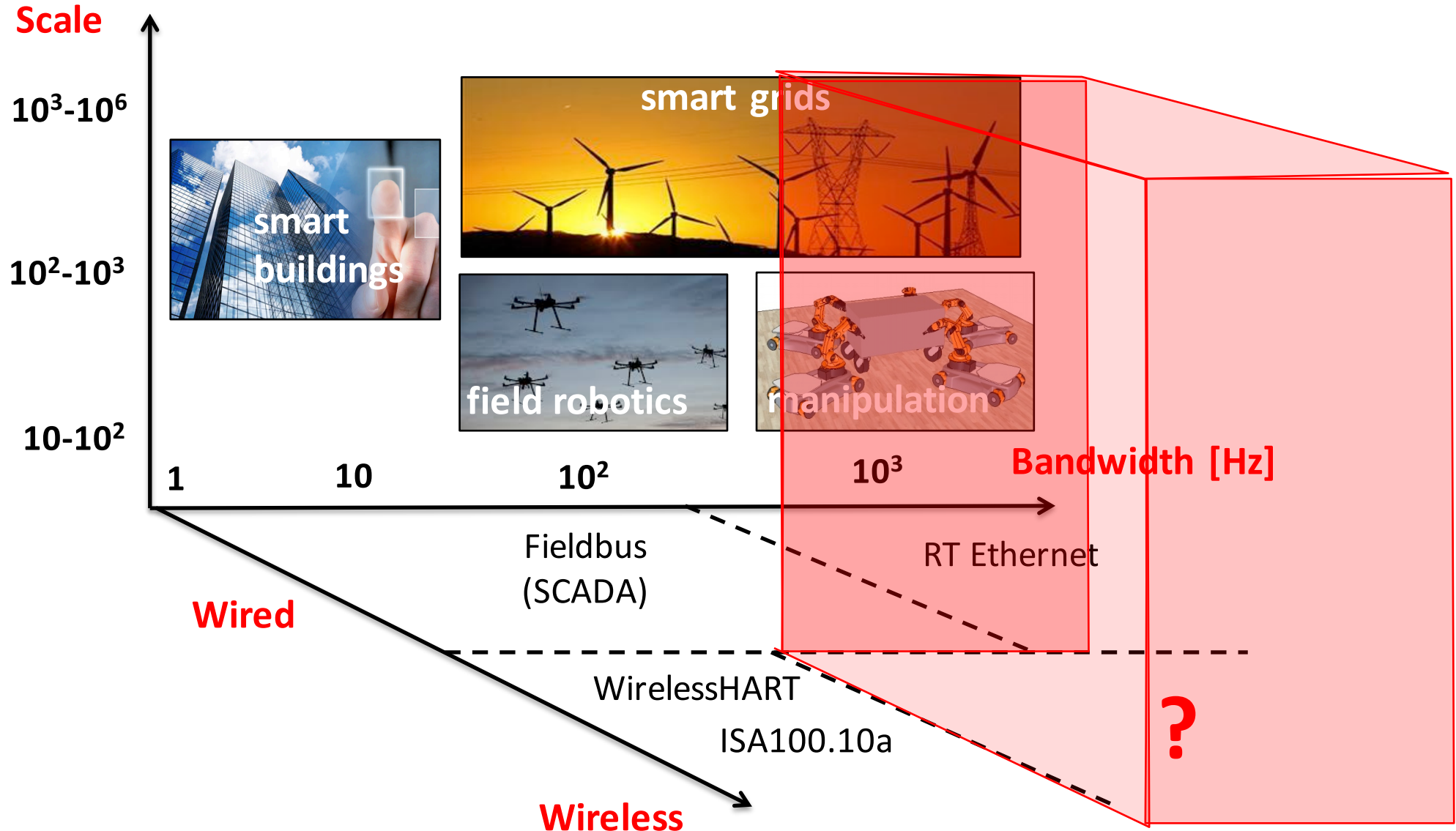
# The XXI century: a Smart World



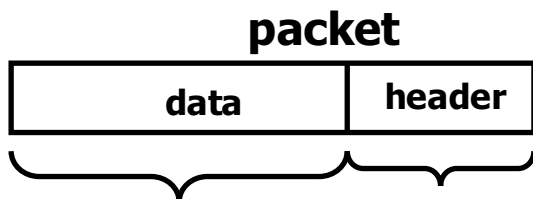
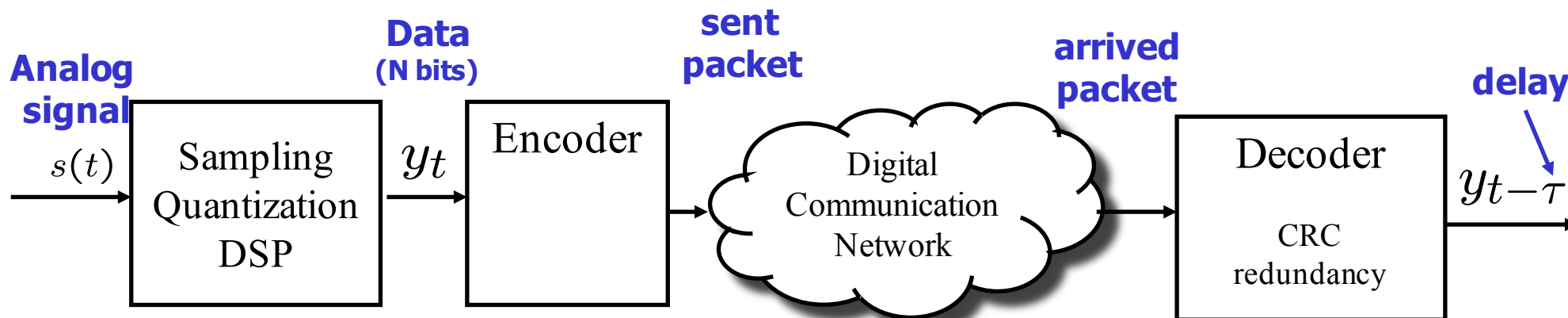
January 2012 | Volume 100 | Number 1  
**Proceedings OF THE IEEE**



# The challenge cube for time-critical smart systems



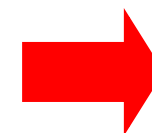
# 20 years ago in Berkeley....



|                  |                      |                  |
|------------------|----------------------|------------------|
| <b>ATM</b>       | <b>384 bits</b>      | <b>40 bits</b>   |
| <b>Ethernet</b>  | <b>&gt;368 bits</b>  | <b>112 bits</b>  |
| <b>Bluetooth</b> | <b>&gt;499 bits</b>  | <b>~100 bits</b> |
| <b>Zigbee</b>    | <b>&lt;1000 bits</b> | <b>128 bits</b>  |

## Assumptions:

- (1) Quantization noise  $\ll$  sensor noise
- (2) Packet-rate limited ( $\neq$  bit-rate)
- (3) No transmission noise (data corrupted=dropped packet)

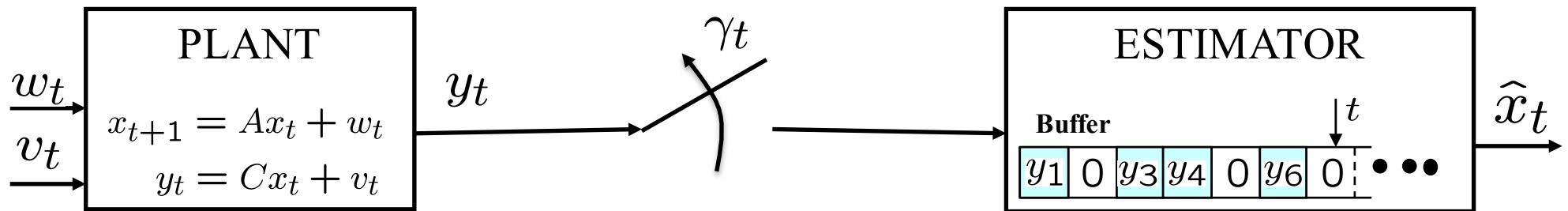


**Packet loss  
at receiver  
&  
Unit delay ( $\tau=1$ )**



# 20 years ago in Berkeley....

$\hat{x}_t = \mathbb{E}[x_t | \{y_k\}]$  available at estimator at time  $t$



$$\gamma_t = \begin{cases} 1 & \text{if } y_t \text{ received at time } t \\ 0 & \text{otherwise} \end{cases}$$

$$\tilde{y}_t = \gamma_t(Cx_t + v_t) = C_t x_t + u_t$$

**Time-varying  
Kalman filter**

$$\hat{x}_t = \mathbb{E}[x_t | \tilde{y}_t, \dots, \tilde{y}_1, \gamma_t, \dots, \gamma_1]$$

# 20 years ago in Berkeley....

B. Sinopoli, L. Schenato, M. Franceschetti, K. Poolla, M.I. Jordan, and S. Sastry. **Kalman filtering with intermittent observations.** *IEEE Transactions on Automatic Control*, 49(9):1453–1464, September 2004

$$\hat{x}_{t+1|t} = A\hat{x}_{t|t-1} + \gamma_t AK_t(y_t - C\hat{x}_{t|t-1})$$

$$K_t = f(P_{t|t-1})$$

$$P_{t+1|t} = \Phi_{\gamma_t}(P_{t|t-1})$$

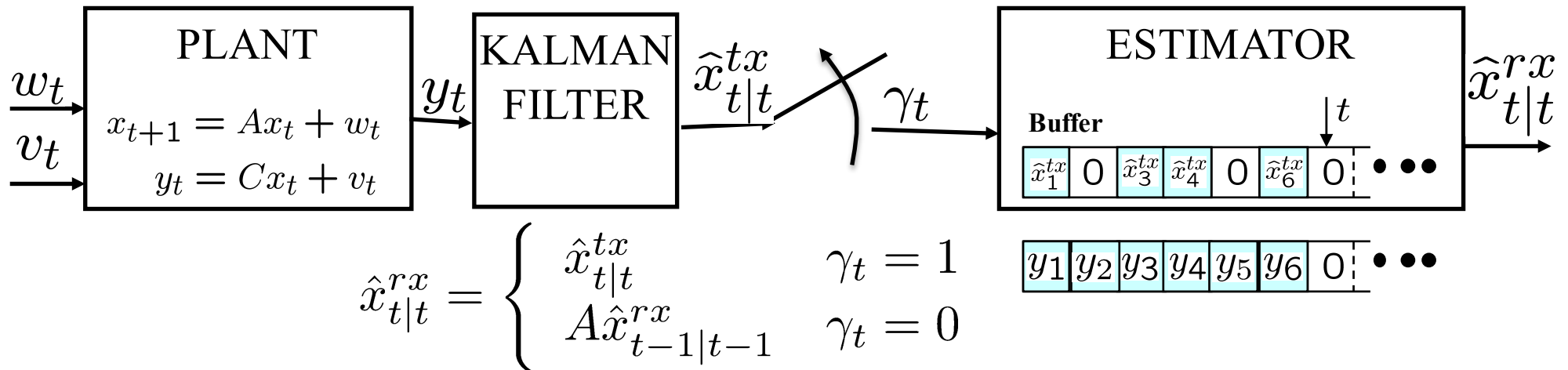
$$\Phi_\epsilon(P) = APA^T + Q - (1 - \epsilon) APC^T (CPC^T + R)^{-1} CPA^T$$

Modified Algebraic  
Riccati Equation (MARE)  
( $\Phi_1(P)=ARE$ )

- Simple to understand but not trivial
- Critical packet loss probability function of eigenvalues of A
- Some new mathematical techniques
- Estimator designed for performance not only stability
- Many open questions remained unanswered

# One open question

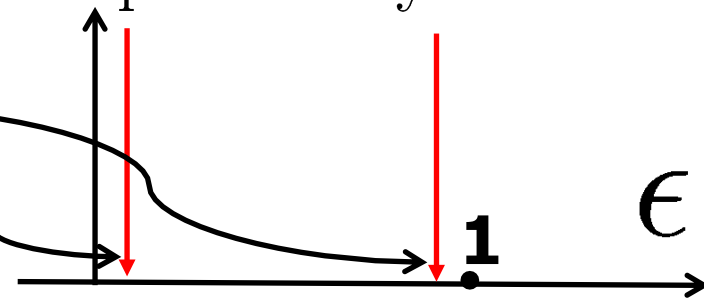
V. Gupta, D. Spanos, B. Hassibi, and R. M. Murray. **Optimal LQG control across a packet-dropping link.** *Systems and Control Letters*, 56(6):439–446, 2007



If  $y \in \mathbb{R}, x \in \mathbb{R}^n$ , then critical packet loss probability  $\epsilon$ .

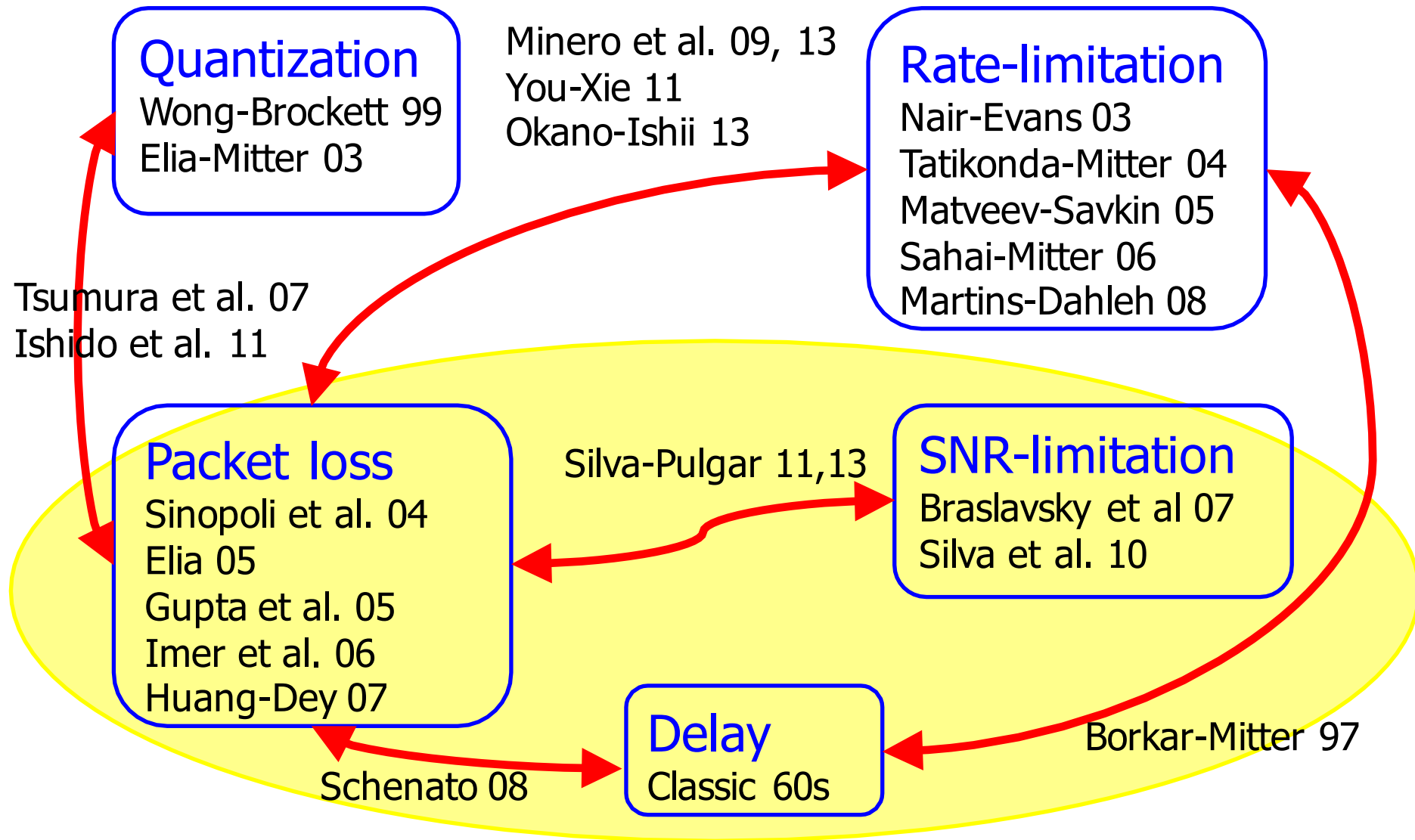
$$\epsilon < \epsilon_x^c = \frac{1}{|\lambda_{max}(A)|^2}: \text{transmit } \hat{x}_t$$

$$\epsilon < \epsilon_y^c = \frac{1}{|\prod \lambda_i^u(A)|^2}: \text{transmit } y_t$$



If  $n=10000$  is it better to send the quantized state rather than the quantized measurement?  $\implies$  need to include quantization

# Previous work







# Joint work with:



**Alessandro Chiuso**

Stochastic Identification  
Univ. of Padova



**Andrea Zanella**

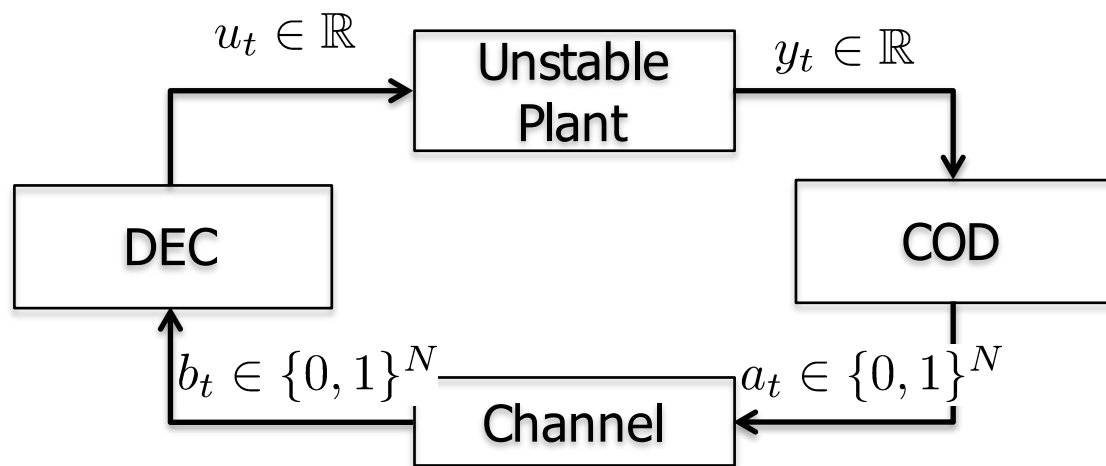
Wireless communications  
Univ. of Padova



**Nicola Laurenti**

Information Theory  
Univ. of Padova

# Modeling

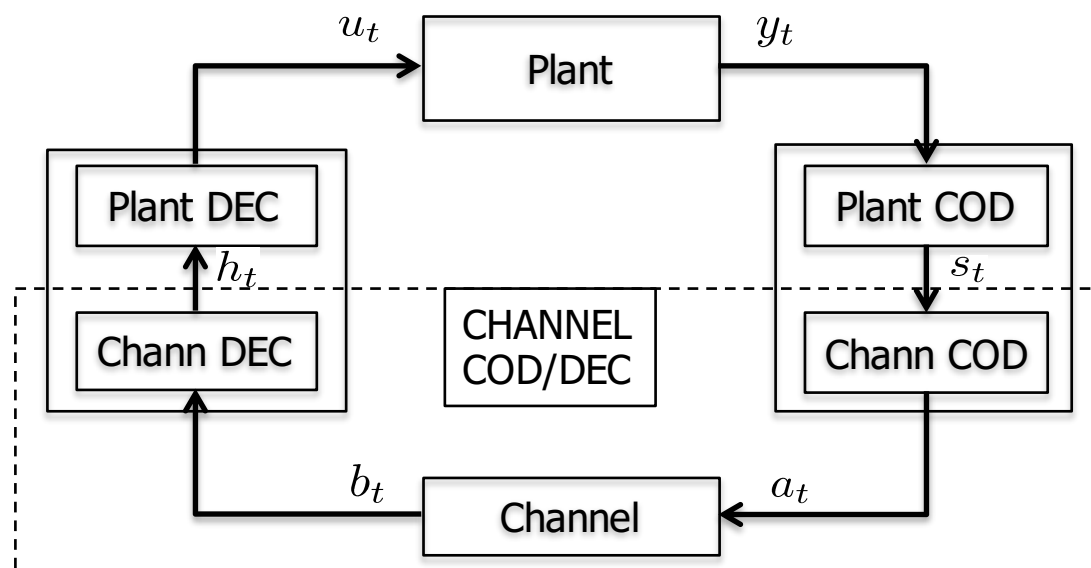


$$x_{t+1} = ax_t + u_t + w_t$$

$$y_t = x_t + v_t$$

$$|a| > 1,$$

$$w_t \sim N(0, \sigma_w^2), v_t \sim N(0, \sigma_v^2)$$



## Proposed approach:

- 1) Separate control/estimation design from communication design.
- 2) Use of traditional coding with finite block-length (different from any-time coding of Sahai-Mitter 07 !!)

Ideally:  $h_t \approx s_t \in \mathbb{R}$

# About coding modeling



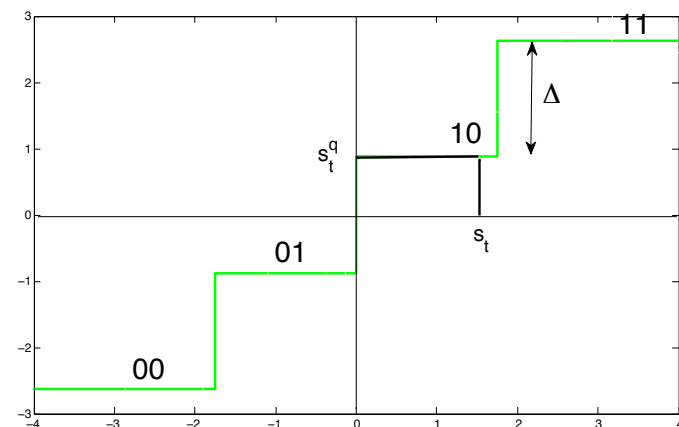
## A naïve coding/decoding scheme:

[10]: symbol to be sent

[10|1]: add parity check bit

$a_t = [111|000|111]$ : add redundancy

Noisy Channel: recovery via majority bits



RECEIVED ( $b_t$ )

[101|100|011]

( $h_t^q = s_t^q$ )

[111|110|111]

[100|110|111]

RECOVERY

[10|1]

[11|1]

[01|1]

DECODED

correct decoding: [10]

erasure

wrong decoding: [01] ( $h_t^q \neq s_t^q$ )

Receiver knows  $\Delta$  and therefore maps [10] into the real number  $h_t$

# About coding modeling



## Role of code length:

$s_t^q = [10]$ : 2-bits of information per period

$a_t = [111|000|111]$ : 9-bit word per period over the channel

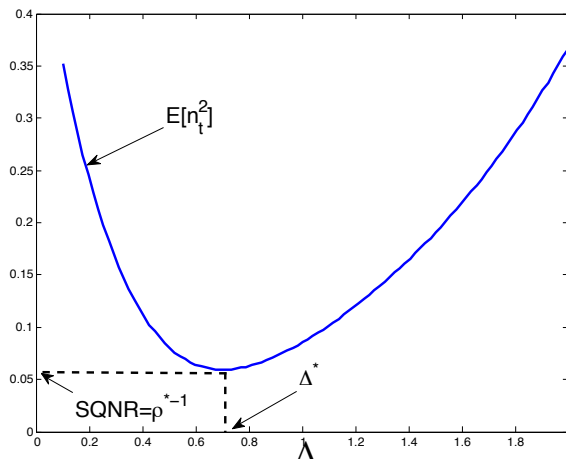
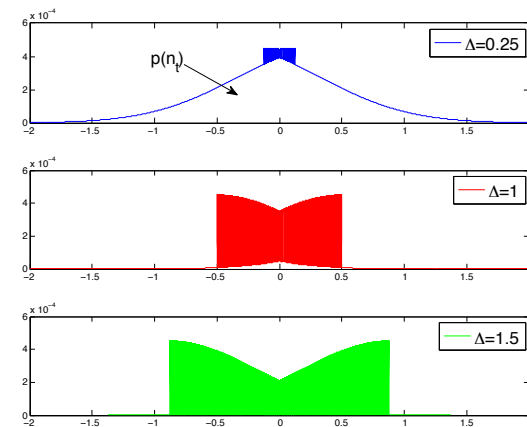
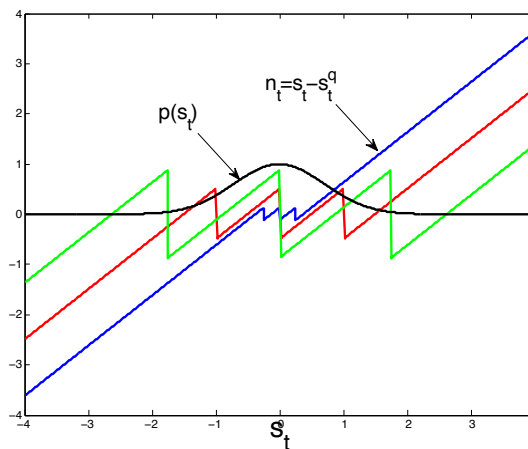
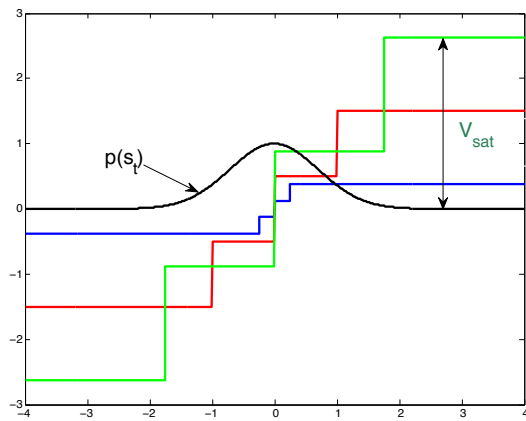
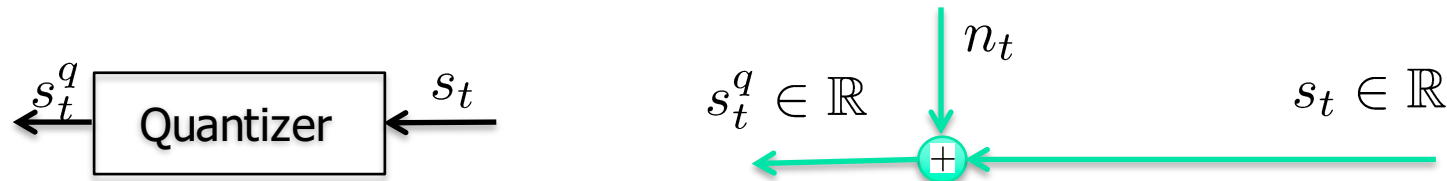
$(s_t^q, s_{t-1}^q) = [11, 10] \rightarrow a_t = [xxx|xxx|xxx|xxx|xxx|xxx]$  smarter coding  
18-bit blocklength over 2 period  $\Rightarrow$  9-bits/period

## Longer block-length:

- Same channel rate (bits/period)
- Smaller erasure probability
- Larger delay



# About quantization modeling



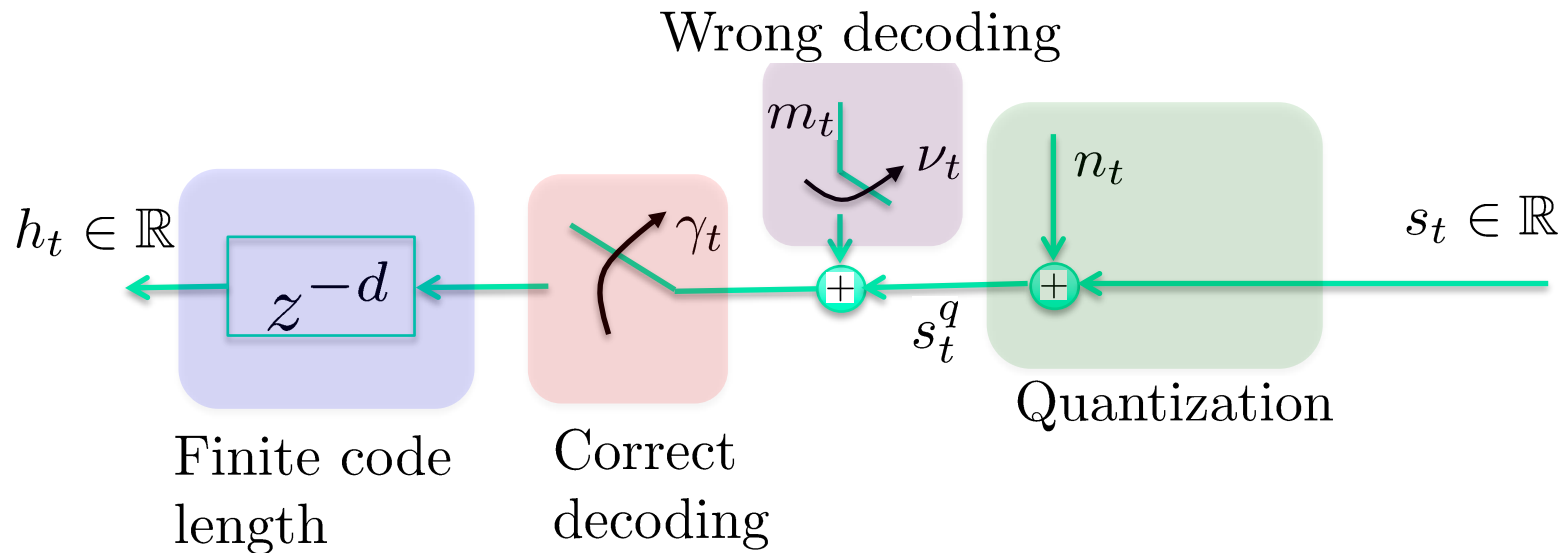
$$\mathbb{E}[n_t^2] = \frac{1}{\rho} \mathbb{E}[s_t^2], \quad \rho: \text{SNR}$$

$$n_t \perp s_t ?$$

D. Marco and D. Neuhoff, "The validity of the additive noise model for uniform scalar quantizers," *IEEE Trans. Info. Theory*, vol. 51, no. 5, pp. 1739–1755, 2005

A. Leong, S. Dey, and G. Nair, "Quantized filtering schemes for multi-sensor linear state estimation: Stability and performance under high rate quantization," *IEEE Trans. Sig. Proc.*, vol. 61, no. 15, pp. 3852–3865, 2013.

# "Analog" channel COD/DEC model



$n_t$ : quantization noise

$\gamma_t = 0, \nu_t = \{0, 1\}$ : undecoded word (erasure)

$\gamma_t = 1, \nu_t = 0$ : correctly decoded word

$\gamma_t = 1, \nu_t = 1$ : wrongly decoded word

$d$ : decoding delay (integer)

$P[\gamma_t = 0] = \varepsilon$ : erasure probability

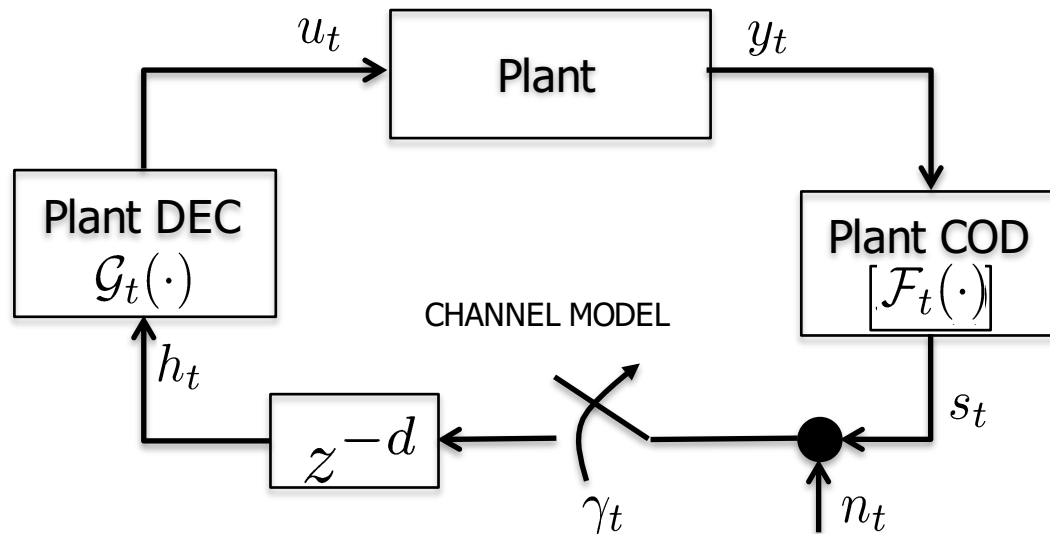
$P[\nu_t = 1] = \varepsilon_w$ : undetected error probability

$\varepsilon_w \ll \varepsilon$

$E[n_t^2] = \frac{1}{\rho} E[s_t^2]$ ,  $\rho$ : SNR

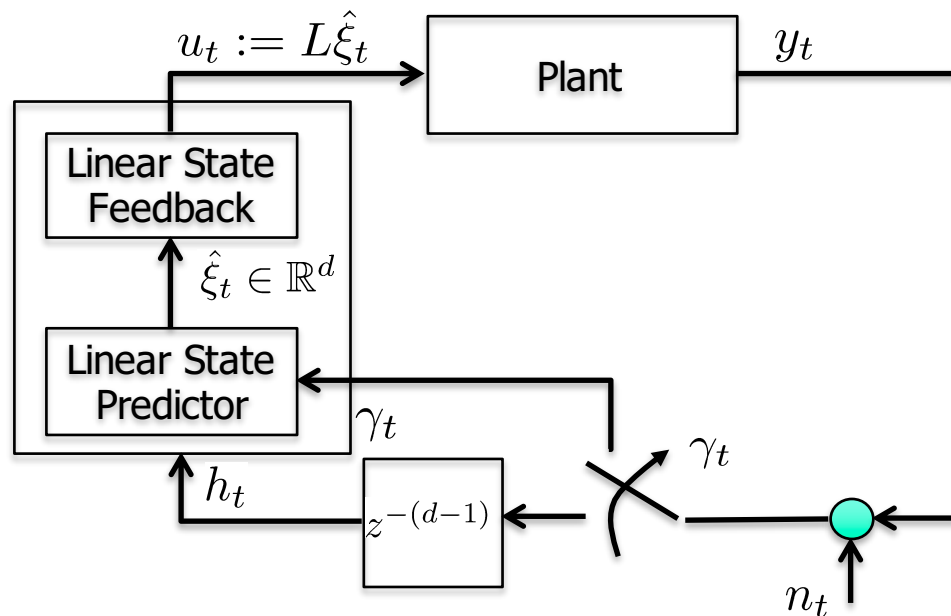
$E[m_t^2] \approx E[s_t^2]$

# Problem formulation



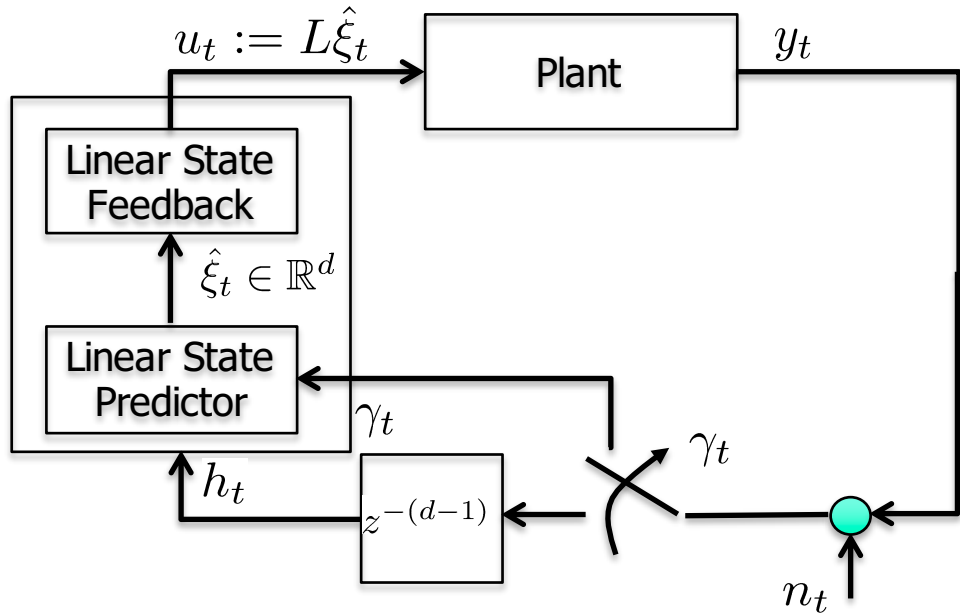
$$x_{t+1} = ax_t + u_t + w_t$$

$$y_t = x_t + v_t$$



1. Scalar dynamics
2. No transmission pre-processing
3. Estimator+ state feedback architecture

# Problem formulation (cont'd)



$$x_{t+1} = ax_t + u_t + w_t$$

$$y_t = x_t + v_t$$

## Augmented System dynamics

$$\underbrace{\begin{bmatrix} x_{t-d+2} \\ \vdots \\ \vdots \\ x_{t+1} \end{bmatrix}}_{\xi_{t+1}} = \underbrace{\begin{bmatrix} 0 & 1 & \cdots & 0 \\ \vdots & \ddots & \ddots & 0 \\ 0 & \cdots & \ddots & 1 \\ 0 & \cdots & 0 & a \end{bmatrix}}_A \underbrace{\begin{bmatrix} x_{t-d+1} \\ \vdots \\ \vdots \\ x_t \end{bmatrix}}_{\xi_t} + \underbrace{\begin{bmatrix} 0 \\ \vdots \\ 0 \\ 1 \end{bmatrix}}_B (u_t + w_t)$$

$$y_t = \underbrace{[0 \ \cdots \ 0 \ 1]}_C \xi_t + v_t$$

$$h_t = \gamma_{t-d+1} \underbrace{([1 \ 0 \ \cdots \ 0])}_H \xi_t + v_{t-d+1} + n_{t-d+1}$$

## Linear estimator + linear controller

$$\hat{\xi}_{t+1} = A\hat{\xi}_t + Bu_t + \gamma_{t-d+1}G(h_t - H\hat{\xi}_t)$$

$$u_t = L\hat{\xi}_t$$

## LQG performance optimization

$$(G^*, L^*) := \operatorname{argmin}_{G, L} \mathbb{E}[y_t^2] + r\mathbb{E}[u_t^2]$$

$$\text{s.t. } \mathbb{E}[n_t^2] = \frac{1}{\rho} \mathbb{E}[y_t^2]$$



# Problem solution

## Augmented System dynamics

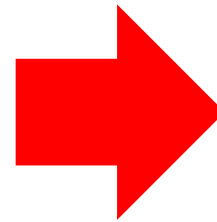
$$\begin{aligned}\xi_{t+1} &= A\xi_t + B(u_t + w_t) \\ y_t &= C\xi_t + v_t \\ h_t &= \gamma_{t-d+1}H(\xi_t + v_{t-d+1} + n_{t-d+1})\end{aligned}$$

## Linear estimator + linear controller

$$\begin{aligned}\hat{\xi}_{t+1} &= A\hat{\xi}_t + Bu_t + \gamma_{t-d+1}G(h_t - H\hat{\xi}_t) \\ u_t &= L\hat{\xi}_t\end{aligned}$$

## LQG performance optimization

$$\begin{aligned}(G^*, L^*) &:= \operatorname{argmin}_{G, L} J(G, L) = \mathbb{E}[y_t^2] + r\mathbb{E}[u_t^2] \\ \text{s.t.} &\quad \mathbb{E}[n_t^2] = \alpha\mathbb{E}[y_t^2]\end{aligned}$$



$$P := \operatorname{Var} \left\{ \begin{bmatrix} \hat{\xi}_t \\ \xi_t - \hat{\xi}_t \end{bmatrix} \right\}$$

$$\begin{aligned}\min_{G, L} & J(P, G, L) \\ \text{s.t.} & P = \mathcal{M}(P, G, L)\end{aligned}$$

$J$  and  $\mathcal{M}$ : linear in  $P$   
"quadratic" in  $G, L$

$$P = \underbrace{(1 - \epsilon)\bar{A}_1 P \bar{A}_1^\top + \epsilon\bar{A}_0 P \bar{A}_0^\top + \sigma_w^2 \bar{B} \bar{B}^\top + \alpha(1 - \epsilon)\bar{G} \bar{C} P \bar{C}^\top \bar{G}^\top + (1 - \epsilon)(1 + \alpha)\bar{G} \sigma_v^2 \bar{G}^\top}_{\mathcal{M}(P, G, L)}$$

# Problem solution

## Solve via Lagrangian

$$\begin{aligned} \min_{P, \Lambda, G, L} \quad & J(P, G, L) + \text{trace}(\Lambda(P - \mathcal{M}(P, G, L))) := \mathcal{L}(P, \Lambda, G, L) \\ \text{s.t.} \quad & P \geq 0, \Lambda \geq 0 \end{aligned}$$



## Necessary optimal conditions

$$\frac{\partial \mathcal{L}}{\partial P} = 0, \quad \frac{\partial \mathcal{L}}{\partial \Lambda} = 0, \quad \frac{\partial \mathcal{L}}{\partial L} = 0, \quad \frac{\partial \mathcal{L}}{\partial G} = 0$$



## Coupled Riccati-like Equations

$$P = \Phi_1(P, \Lambda)$$

$$\Lambda = \Phi_2(P, \Lambda)$$

$$G = \Psi_1(P)$$

$$L = \Psi_2(\Lambda)$$

# Further simplification

## Coupled Riccati-like Equations

$$P = \Phi_1(P, \Lambda)$$

$$\Lambda = \Phi_2(P, \Lambda)$$

$$G = \Psi_1(P)$$

$$L = \Psi_2(\Lambda)$$



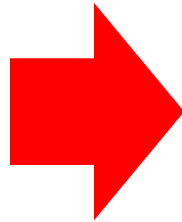
$$\underbrace{\begin{bmatrix} x_{t-d+2} \\ \vdots \\ \vdots \\ x_{t+1} \end{bmatrix}}_{\xi_{t+1}} = \underbrace{\begin{bmatrix} 0 & 1 & \cdots & 0 \\ \vdots & \ddots & \ddots & 0 \\ 0 & \cdots & \ddots & 1 \\ 0 & \cdots & 0 & a \end{bmatrix}}_A \underbrace{\begin{bmatrix} x_{t-d+1} \\ \vdots \\ \vdots \\ x_t \end{bmatrix}}_{\xi_t} + \underbrace{\begin{bmatrix} 0 \\ \vdots \\ 0 \\ 1 \end{bmatrix}}_B (u_t + w_t)$$

$$y_t = \underbrace{[0 \ \cdots \ 0 \ 1]}_C \xi_t + v_t$$

$$h_t = \gamma_{t-d+1} \underbrace{([1 \ 0 \ \cdots \ 0])}_H \xi_t + v_{t-d+1} + n_{t-d+1}$$

$$L = \begin{bmatrix} 0 & 0 & \cdots & 0 & \ell \end{bmatrix}$$

$$G = \begin{bmatrix} g & ag & \cdots & a^{d-1}g \end{bmatrix}^T$$



For  $r = 0$  problem equivalent to the solution of a scalar Riccati-like equation:

$$p = a^2 p + \sigma_w^2 - \delta \frac{a^2 p^2}{p + \bar{r}(d)}$$

$$\delta := \frac{1 - \epsilon}{1 + \alpha a^{2d}}$$



# Further simplification

$$p = a^2 p + \sigma_w^2 - \delta \frac{a^2 p^2}{p + \bar{r}(d)}$$

$$\delta := \frac{1 - \epsilon}{1 + \alpha a^{2d}}$$



B. Sinopoli, L. Schenato, M. Franceschetti, K. Poolla, M.I. Jordan, and S. Sastry. **Kalman filtering with intermittent observations.** *IEEE Transactions on Automatic Control*, 49(9):1453–1464, September 2004

Necessary and sufficient stability for  $r \geq 0$ :

$$\frac{1 - \epsilon}{1 + \alpha a^{2d}} > 1 - \frac{1}{a^2}$$

$d$ : decoding delay

$\epsilon$ : erasure probability

$\alpha = \frac{1}{SNR}$ : noise-to-signal ratio



# Discussion w/ related works

$$\frac{1-\epsilon}{1+\alpha a^{2d}} > 1 - \frac{1}{a^2}$$

1) Infinite resolution ( $\alpha=0$ ) and no delay ( $d=0$ ):

$$1 - \epsilon > 1 - \frac{1}{a^2}$$

B. Sinopoli, L. Schenato, M. Franceschetti, K. Poolla, M.I. Jordan, and S. Sastry. **Kalman filtering with intermittent observations**. *IEEE Transactions on Automatic Control*, 49(9):1453–1464, September 2004

2) Infinite resolution ( $\alpha=0$ ) and with delay ( $d>0$ ):

$$1 - \epsilon > 1 - \frac{1}{a^2}$$

L. Schenato. **Kalman filtering for networked control systems with random delay and packet loss**. *IEEE Transactions on Automatic Control*, 53:1311–1317, 2008

3) No packet loss ( $\epsilon=0$ ) and no delay ( $d>0$ ):

$$SNR = \frac{1}{\alpha} > a^2 - 1$$

J.H. Braslavsky, R.H. Middleton, and J.S. Freudenberg. **Feedback stabilization over signal-to-noise ratio constrained channels**. *IEEE Transactions on Automatic Control*, 52(8), 2007

Recalling the rate  $R = \frac{1}{2} \log(1 + SNR)$  and  $R < C$ :

$$C > \log |a|$$

S. Tatikonda and S. Mitter. **Control under communication constraints**. *IEEE Transaction on Automatic Control*, 49(7):1056–1068, July 2004.

# Discussion w/ related works

$$\frac{1-\epsilon}{1+\alpha a^{2d}} > 1 - \frac{1}{a^2}$$

4) No packet loss ( $\epsilon=0$ ) and delay ( $d=1$ ):

$$SNR = \frac{1}{\alpha} > a^4 - a^2$$

J.H. Braslavsky, R.H. Middleton, and J.S. Freudenberg. **Feedback stabilization over signal-to-noise ratio constrained channels.** *IEEE Transactions on Automatic Control*, 52(8), 2007

5) Infinite resolution ( $\alpha=0$ ), packet loss as SNR-limitation + delay

$$\frac{1-\epsilon}{1+\epsilon(a^{2d}-1)} > 1 - \frac{1}{a^2}$$

E.I. Silva and S.A. Pulgar. **Performance limitations for single-input LTI plants controlled over SNR constrained channels with feedback.** *Automatica*, 49(2), 2013

$$1 - \epsilon > 1 - \frac{1}{a^2}$$

Our condition less stringent and independent of delay

6) Rate-limited with delay ( $d=1$ ):

$$R = \frac{1}{2} \log(1 + SNR)$$

$$\mathbb{E} \left[ \left( \frac{a^2}{2^{2R_t}} \right)^n \right] < 1$$

$$R_t = R\delta_t, \delta_t \sim \mathcal{B}(1 - \epsilon)$$



$$\frac{a^2}{1+\rho} (1 - \epsilon) + a^2\epsilon < 1$$

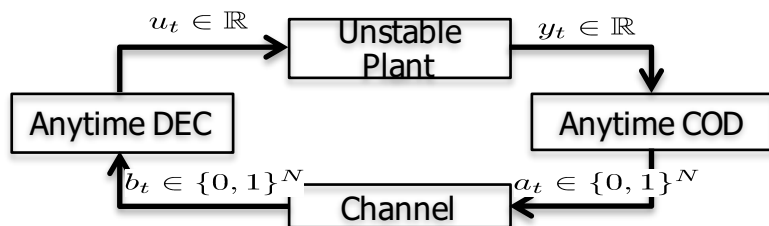
P. Minero, L. Coviello, and M. Franceschetti. **Stabilization over Markov feedback channels: The general case.** *Transactions on Automatic Control*, 58(2):349–362, 2013

# Discussion w/ related works

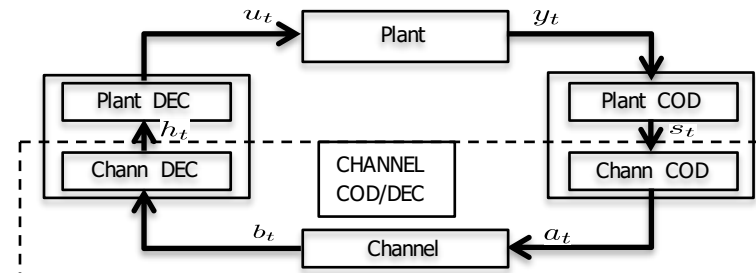
$$\frac{1-\epsilon}{1+\alpha a^{2d}} > 1 - \frac{1}{a^2}$$

## 6) Relation with sequential coding (any-time capacity)

### Anytime coding/decoding



### Fixed-length codes (our approach)



Necessary for optimality:

A. Sahai and S. Mitter. **The necessity and sufficiency of anytime capacity for control over a noisy communication link: Part I.** *IEEE Transaction on Information Theory*, 2006

# What is the role of capacity?

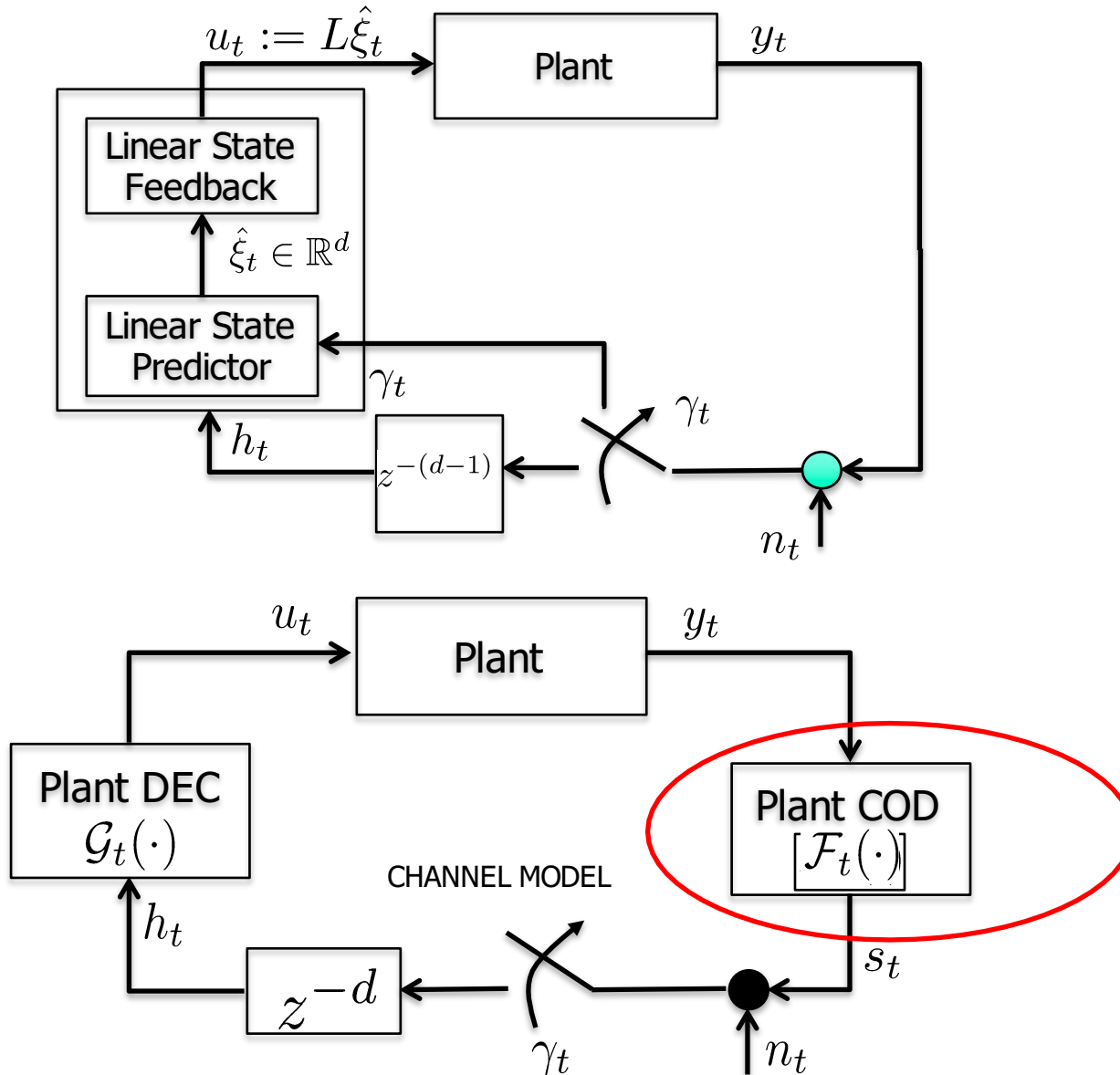
$SNR, d, \epsilon$  are not independent

$$\begin{aligned} a^*(\mathcal{C}) &:= \max_{SNR, d, \epsilon} |a| \\ s.t. & \frac{1-\epsilon}{1+\frac{a^{2d}}{SNR}} > 1 - \frac{1}{a^2} \\ & (SNR, d, \epsilon) \in \Omega(\mathcal{C}) \end{aligned}$$

Feasible set which depends on channel parameters

Y. Polyanskiy, H.V. Poor, and S. Verdú. **Channel coding rate in the finite blocklength regime.** *IEEE Transactions on Information Theory*, 56(5):2307-2359, 2010

# Can we do better with Plant COD?





# Joint work with:

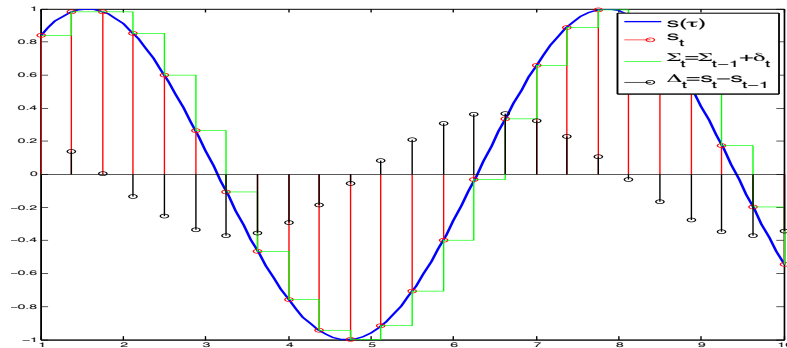
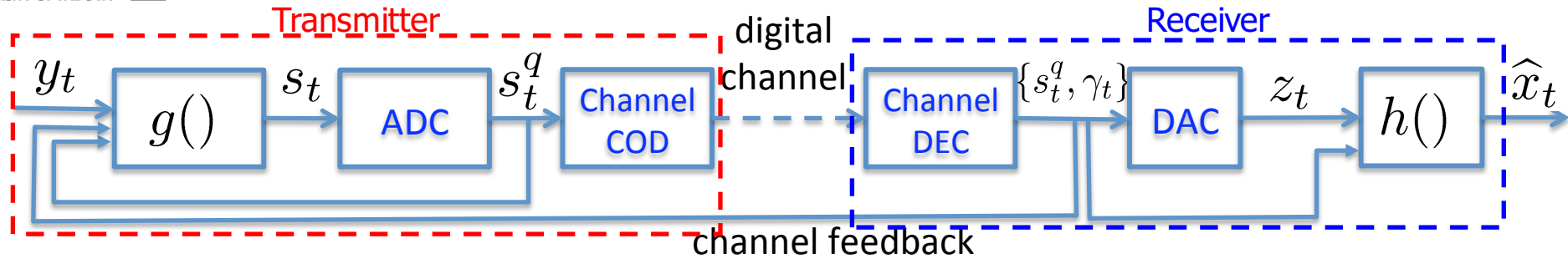


**Alessandro Chiuso**  
Stochastic Identification



**Subhrakanti Dey**  
Wireless communications

# Remote estimation subject to quantization and packet loss



## "Delta-Sigma" modulation:

$\Delta_t = y_t - y_{t-1}$  at the transmitter

$\Sigma_t = \Sigma_{t-1} + \Delta_t$  at the receiver

If  $\Sigma_0 = y_0$  then  $\Sigma_t = y_t$  for all  $t$

July 29, 1952

C. C. CUTLER

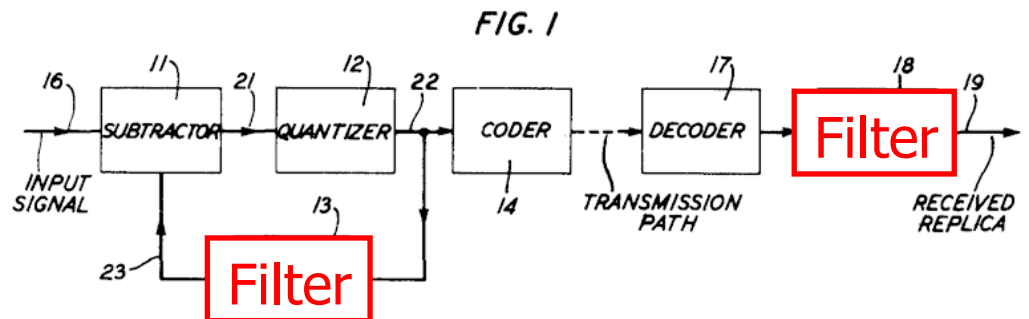
2,605,361

DIFFERENTIAL QUANTIZATION OF COMMUNICATION SIGNALS

Filed June 29, 1950

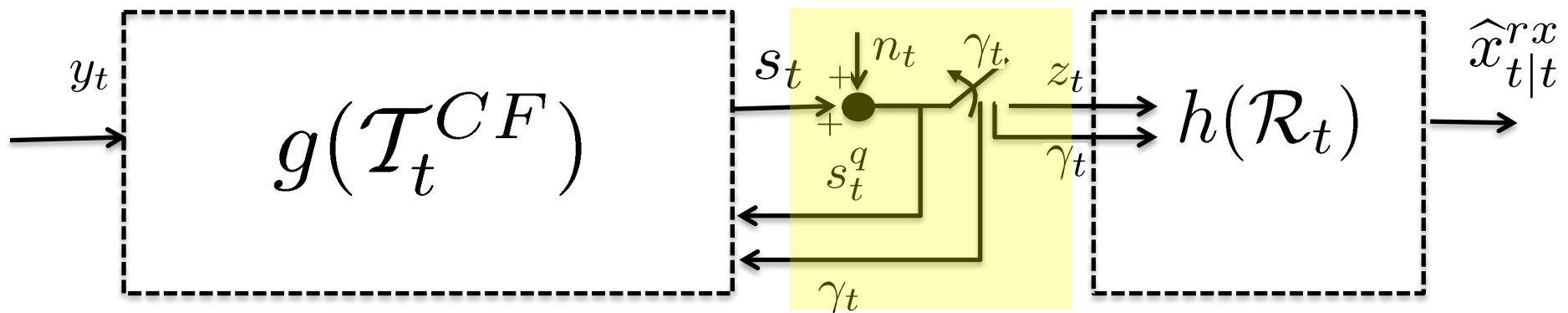
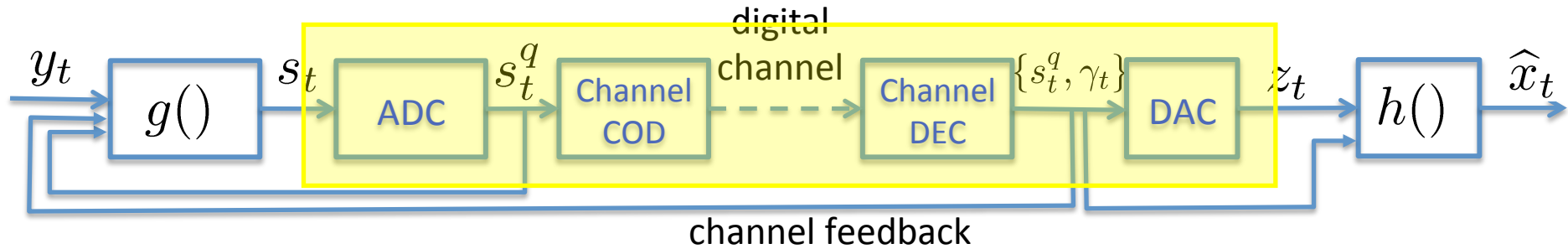
3 Sheets-Sheet 1

## Differential pulse-code modulation (DPCM)





# Remote estimation subject to quantization and packet loss



Information set **with** channel feedback (ACK/NACK)

Information set at receiver

$$\mathcal{T}_t^{CF} = \{y_t, \dots, y_0, s_{t-1}, \dots, s_0, n_{t-1}, \dots, n_0, \gamma_{t-1}, \dots, \gamma_0\}$$

$$\mathcal{R}_t := \{z_t, \dots, z_0, \gamma_t, \dots, \gamma_0\}$$

Information set **without** channel feedback (ACK/NACK)

$$\mathcal{T}_t^{NCF} = \{y_t, \dots, y_0, s_{t-1}, \dots, s_0, n_{t-1}, \dots, n_0\}$$

Goal: minimize error variance  
 $\mathbb{E}[(x_{t+1} - \hat{x}_{t+1|t}^{rx})^2]$

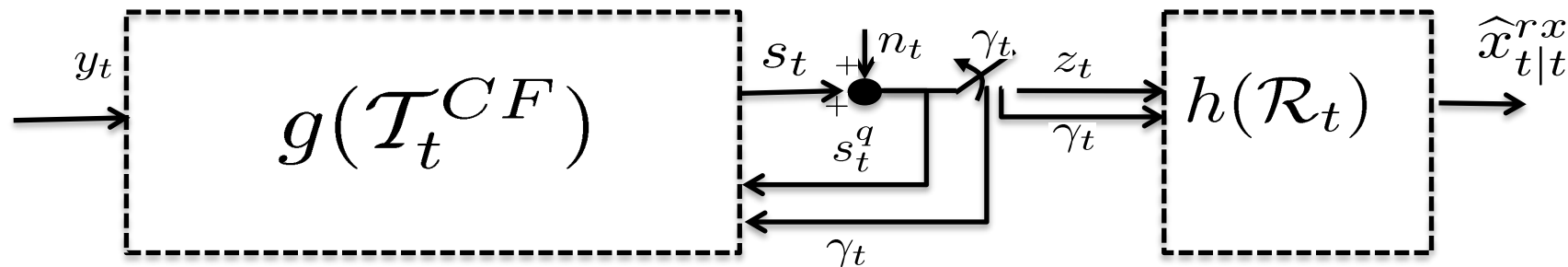
# What is the optimal strategy with channel feedback ?

$$x_{t+1} = ax_t + w_t, \text{ scalar system}$$

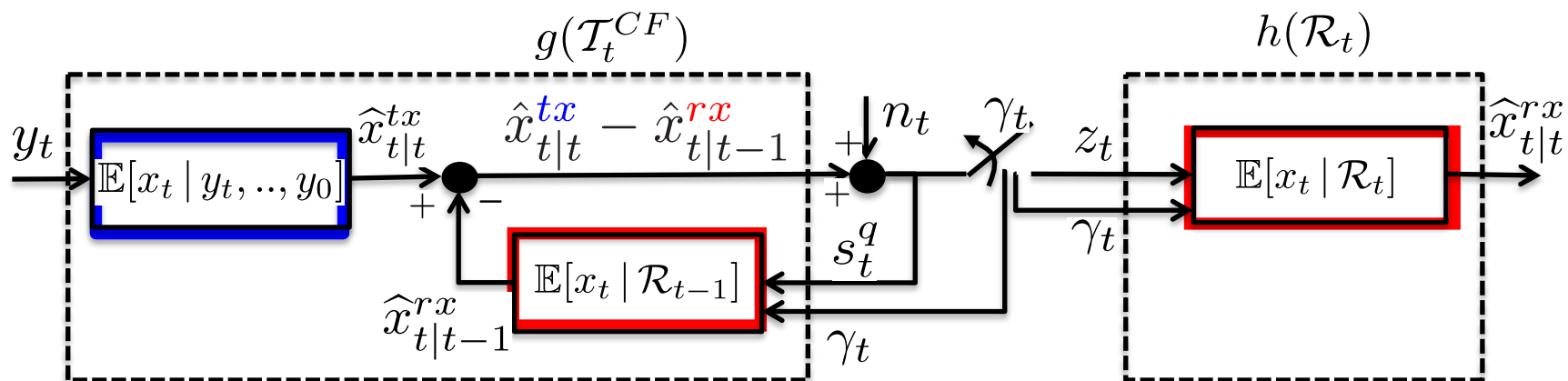
$$y_t = x_t + v_t$$

$$|a| < 1, \text{ stable source}$$

$$\mathcal{T}_t^{CF} \supset \mathcal{R}_{t-1}$$



Optimal strategy (among linear strategies): send innovation



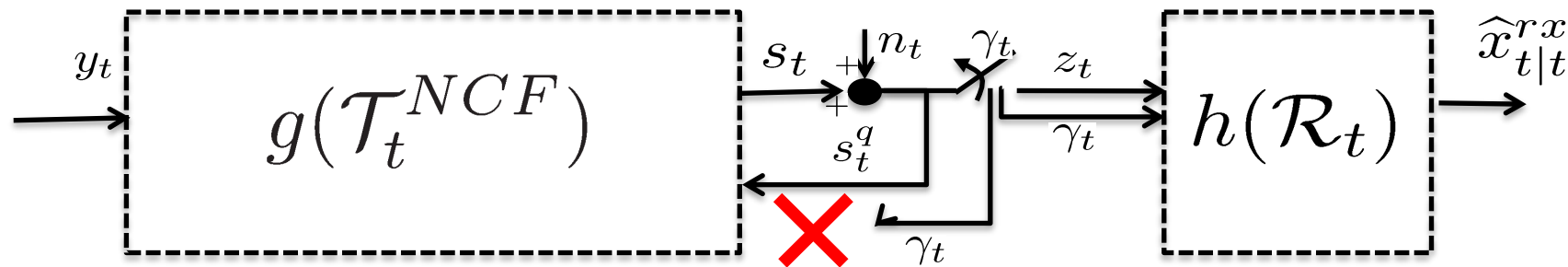
# What is the optimal strategy with no channel feedback ?

$$x_{t+1} = ax_t + w_t, \text{ scalar system}$$

$$y_t = x_t + v_t$$

$$|a| < 1, \text{ stable source}$$

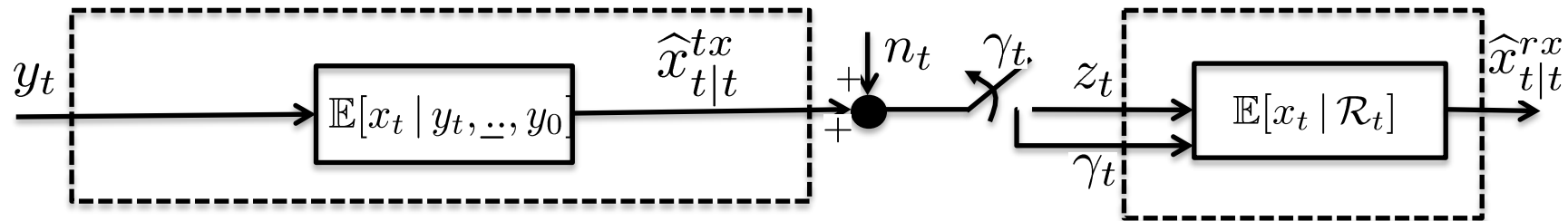
$$\mathcal{T}_t^{NCF} \not\subseteq \mathcal{R}_{t-1}$$



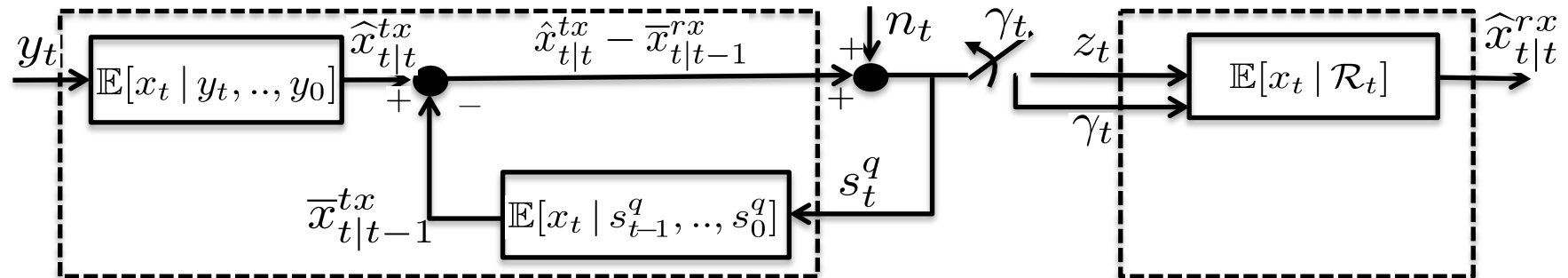
Optimal strategy ? not clear, likely non-linear  
Approach: reasonable suboptimal strategies

# Suboptimal strategies

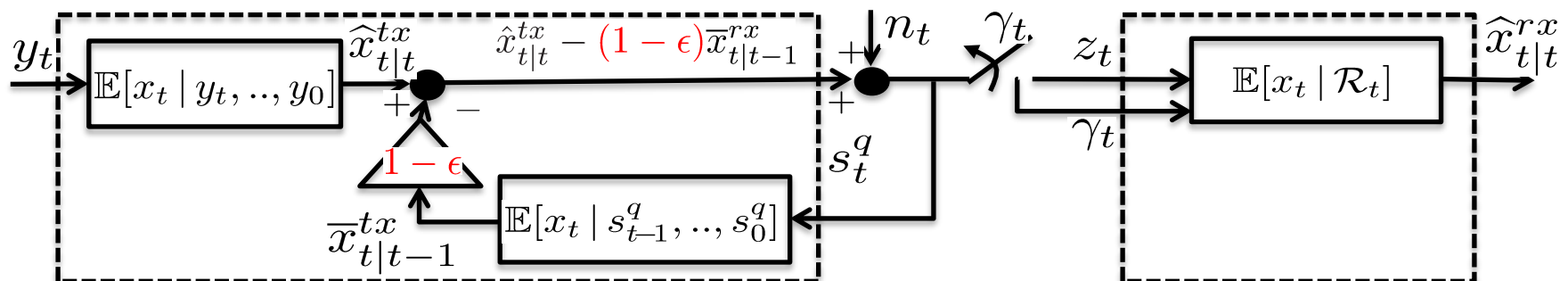
## 1) Estimated state forwarding (Kalman estimate)



## 2) Innovation forwarding assuming no packet loss

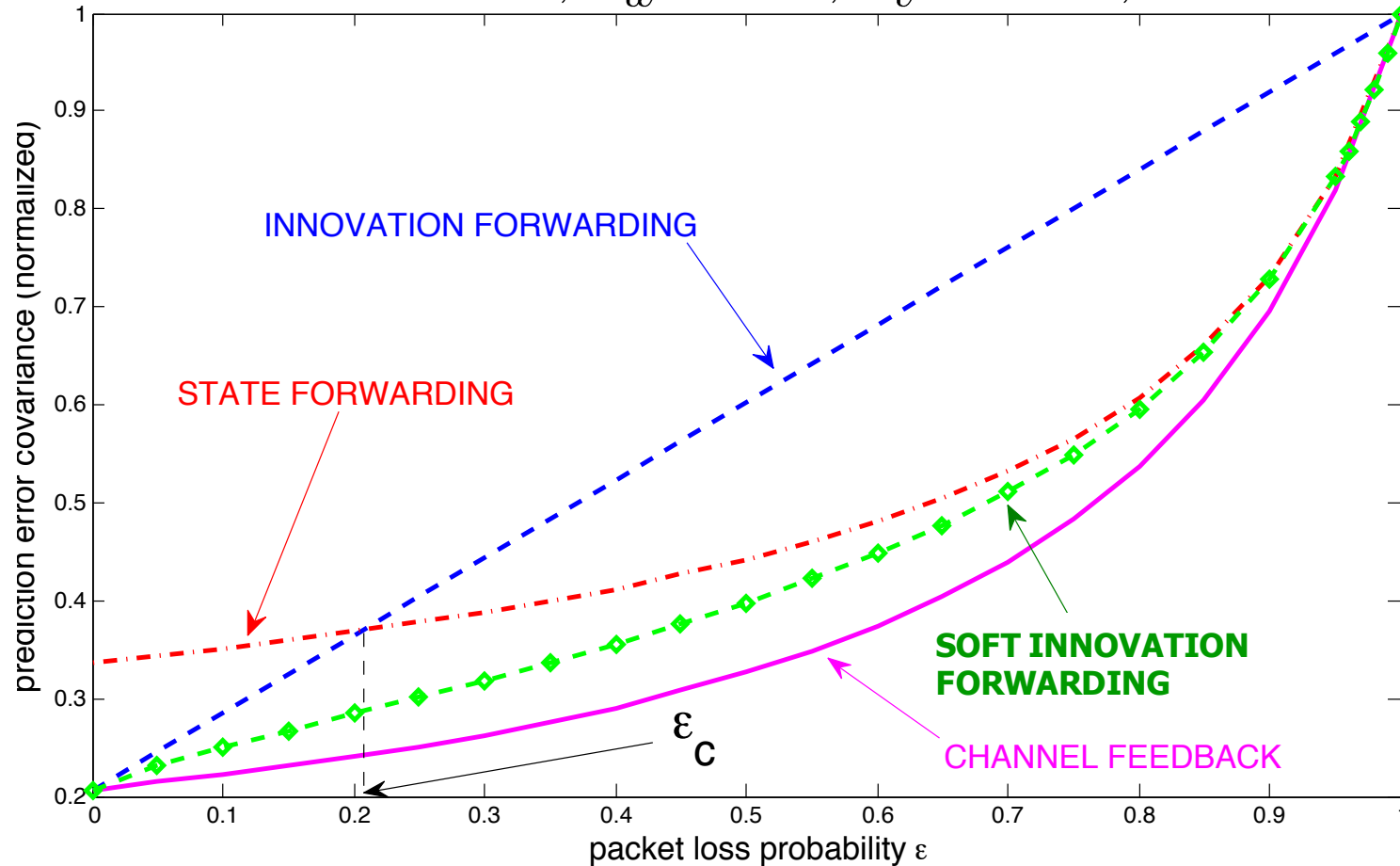


## 3) Hybrid strategy: soft innovation forwarding



# Analytical results

$$SNR = 3, \sigma_w^2 = 0.1, \sigma_v^2 = 0.05, a = 0.95$$



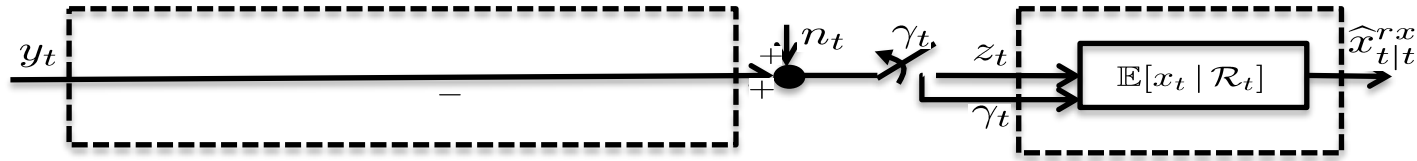
S. Dey, A. Chiuso, L. Schenato. **Feedback Control over lossy SNR-limited channels: linear encoder-decoder-controller design.** *IEEE Transactions on Automatic Control*, vol. 62(6), pp. 3054-3061, 2017

S. Dey, A. Chiuso, L. Schenato. **Remote estimation with noisy measurements subject to packet loss and quantization noise.** *IEEE Transactions on Control of Network Systems*, vol. 1(3), pp. 204-217, 2014

# A unexpected result

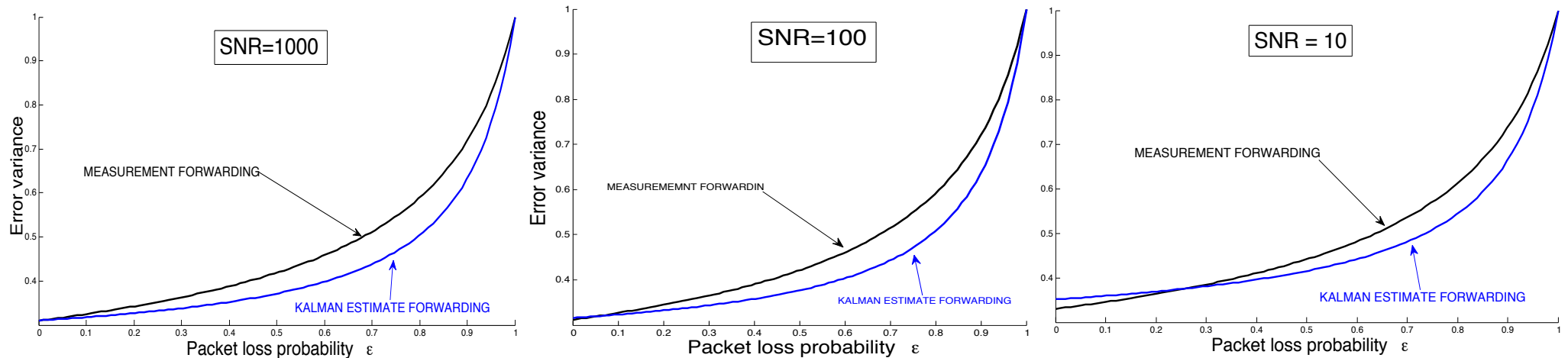
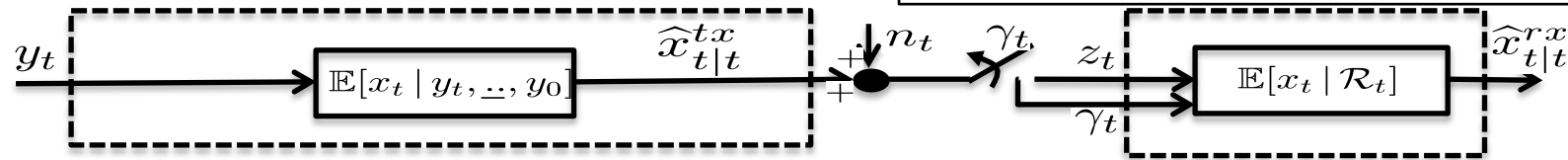
## 1) Measurement forwarding

B. Sinopoli, L. Schenato, M. Franceschetti, K. Poola, M.I. Jordan, and S. Sastry. **Kalman filtering with intermittent observations.** *IEEE Transactions on Automatic Control*, 49(9):1453–1464, September 2004



## 2) Kalman estimate forwarding

V. Gupta, D. Spanos, B. Hassibi, and R. M. Murray. **Optimal LQG control across a packet-dropping link.** *Systems and Control Letters*, 56(6):439–446, 2007



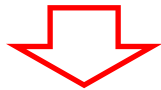
# Is mean square stability relevant?

$$x_{k+1} = ax_k + u_k + w_k, \quad w_k \sim N(0, 1)$$

$$y_k = \gamma_k x_k, \quad \gamma_k \sim \mathcal{B}(1 - \epsilon) \quad \epsilon: \text{packet loss probability, i.e. } \epsilon = \mathbb{P}[\gamma_k = 0]$$

$$u_k = -kx_k$$

$$p_k = E[x_k^2], \quad \text{second moment}$$



$$p_{k+1} = (\epsilon a^2 + (1 - \epsilon)(a - k)^2)p_k + 1$$

$\epsilon = 0$  stochastic linear systems

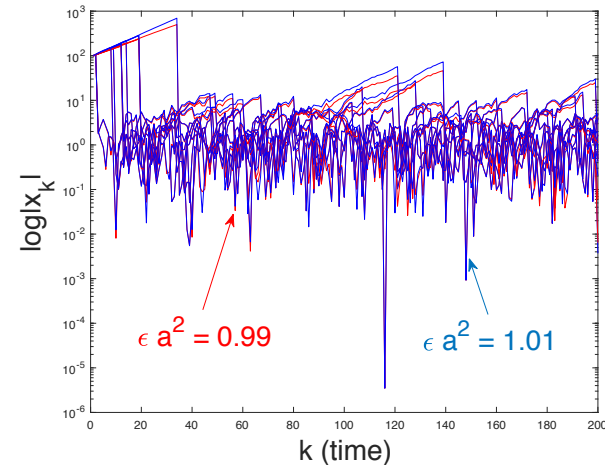
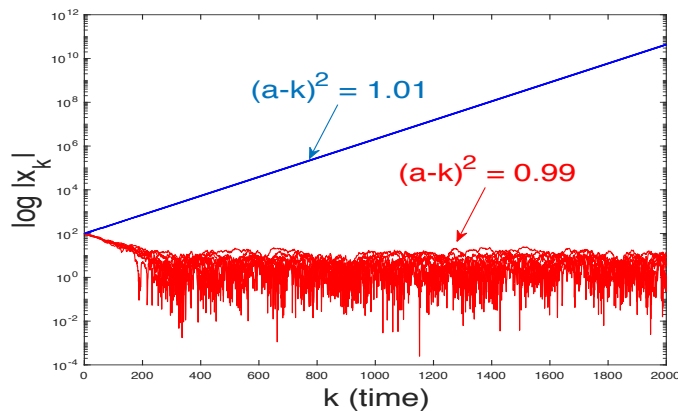
$\epsilon > 0, k = a$  stability for lossy feedback

$$(a - k)^2 < 1$$

$$\epsilon a^2 < 1$$

$$\text{(mean square) stability}$$

$$\epsilon a^2 + (1 - \epsilon)(a - k)^2 < 1$$



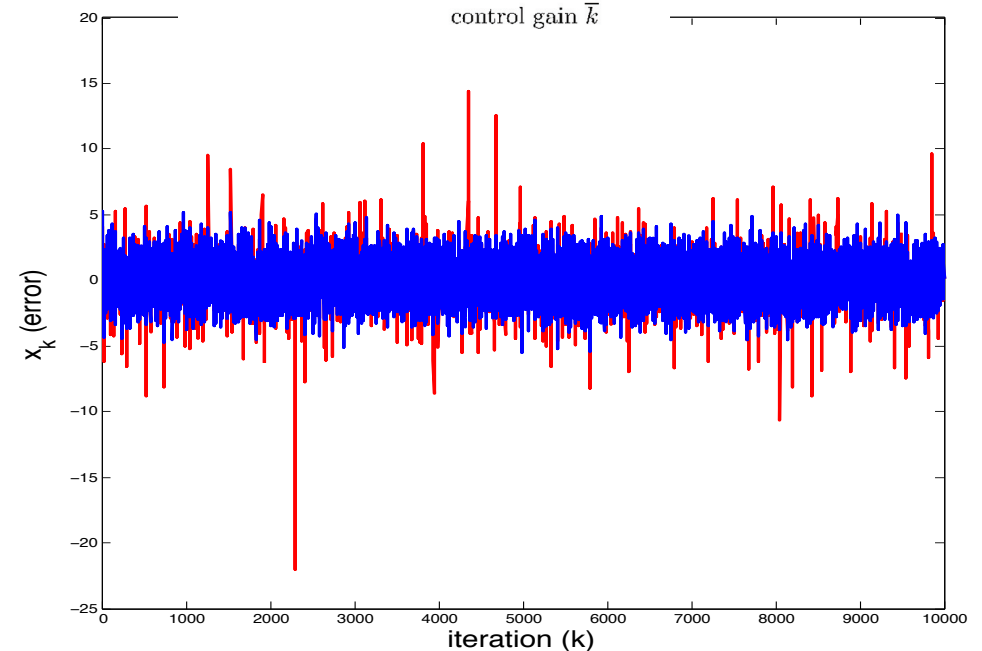
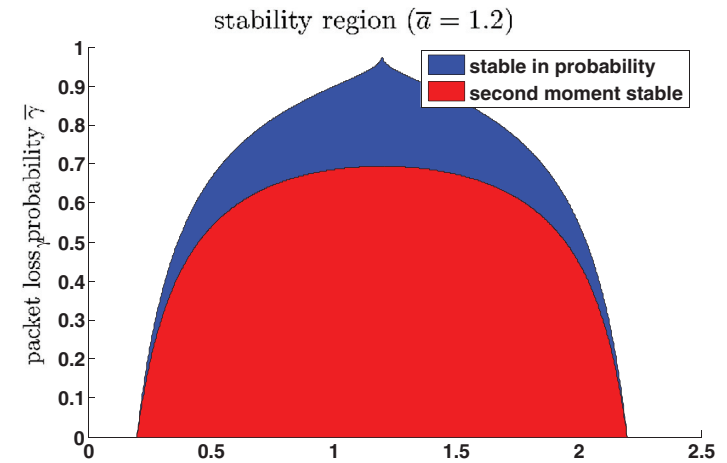
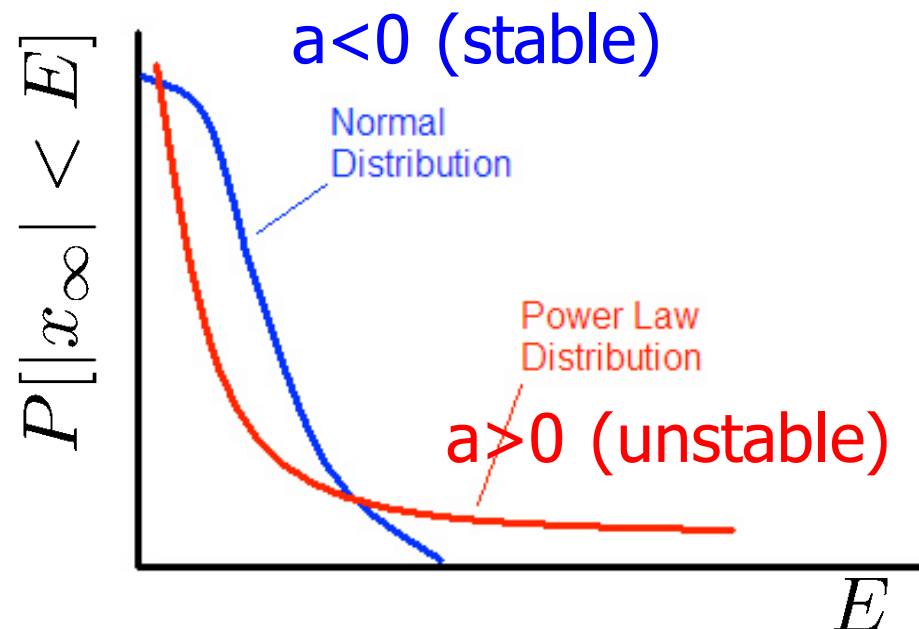
# Non-intuitive answers:

## heavy tail (power-law distribution)

Stochastic **switching** linear systems  
with one unstable system:  
**HEAVY TAIL DISTRIBUTION!!!**

A. Brandt, The stochastic equation  $y_{n+1} = a_n y_n + b_n$  with stationary coefficients, *Adv. Appl. Prob.* 18 (1986) 211–220.

C. Goldie, Implicit renewal theory and tails of solutions of random equations, *Ann. Appl. Probab.* 1 (1) (1991) 126–166.







# Control over wireless: a retrospect 20 years later

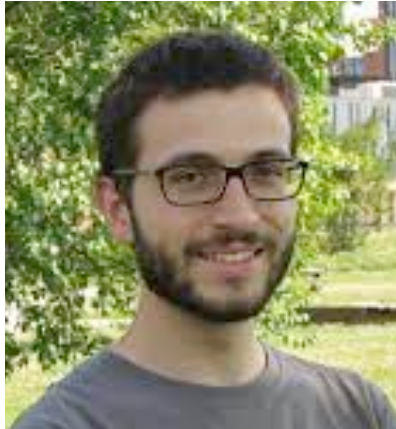
- Scientific impact: one of the most active and cited area in control
- Industrial impact: marginal
- Why?
  - The right tools (model-based control) for the wrong objective (stability)
  - Legacy control systems: PIDs (modeless or emulation-based)
  - No real need .... yet

# Control over wireless: an outlook for the future

- Industry 4.0
  - reconfigurable factory
- UAVs based applications
  - infrastructure maintenance, load transportation, delivery
- Theoretical challenges?
  - Multi-agent cooperation over lossy nets: stability replaced by constraint satisfaction
  - 1Khz bandwidth range (manipulation)
  - Adaptive communication for control (RT-WiFi/5G)



# Preliminary results: remote stabilization via Drive-by-Wi-Fi



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Embedded Control Systems  
Univ. of Padova



**Stefano Vitturi**  
Industrial Communications  
CNR, Italy



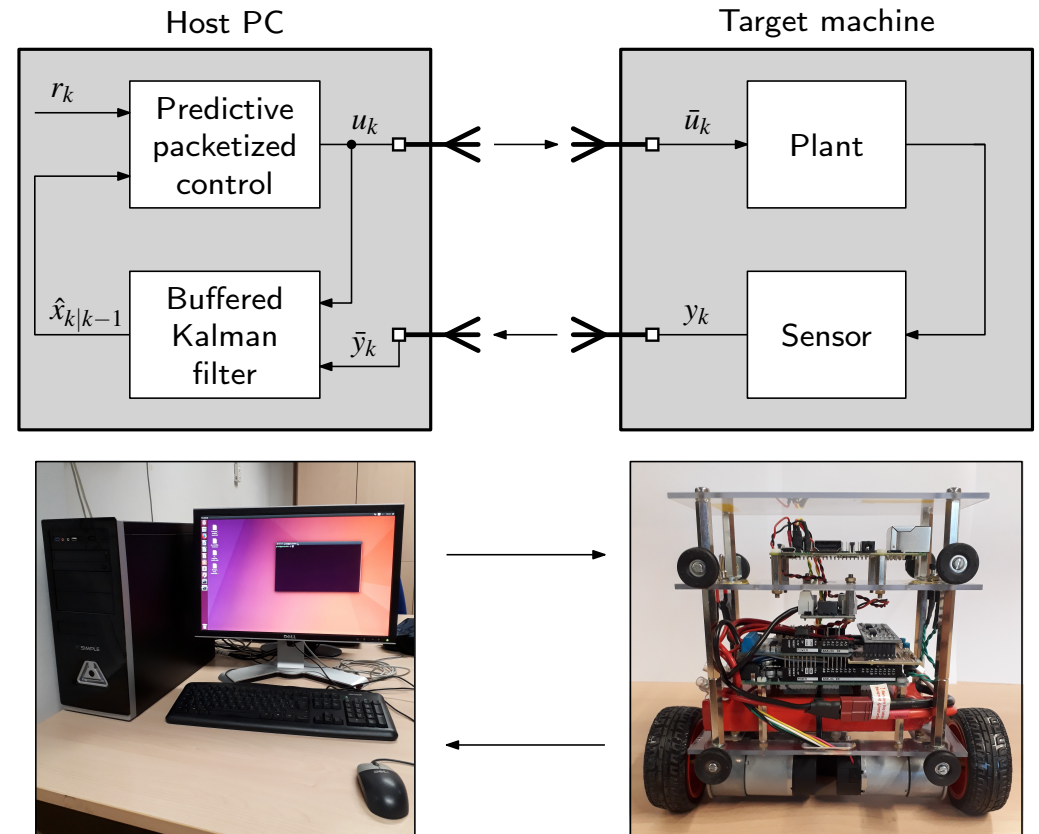
**Federico Tramarin**  
Industrial Communications  
Univ. of Modena, Italy



**Matthias Pezzutto**  
Ph.D. student  
Univ. of Padova

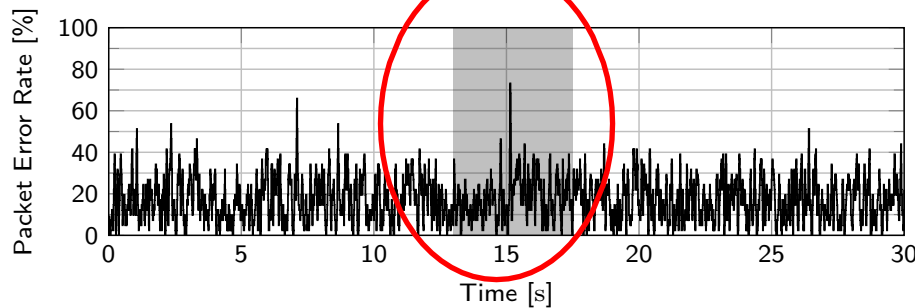
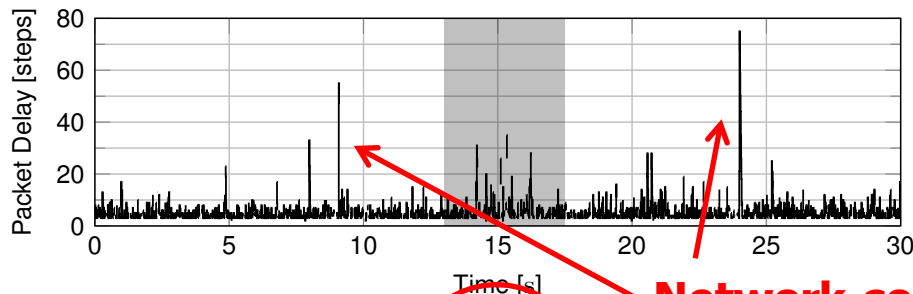
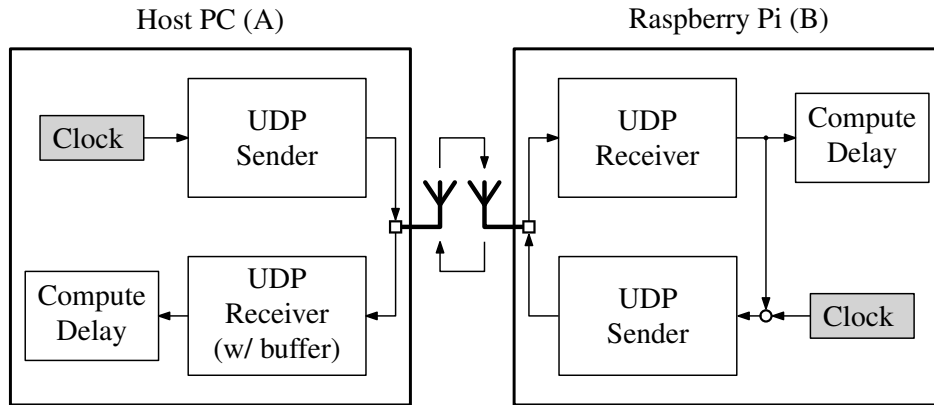
# Preliminary results: remote stabilization via Drive-by-Wi-Fi

- Commercial Off-the-Shelf HW & SW
  - Homemade Segway with gyros, accelerometers, wheel encoders
  - Raspberry Pi (on segway)
  - Linux w/ Matalab on PC
  
- Model-based architecture:
  - Buffered Kalman Filter
  - Predictive packetized control
  
- Industrial environment
  - Multiple Wi-Fi source interference
  - Additional injected noise

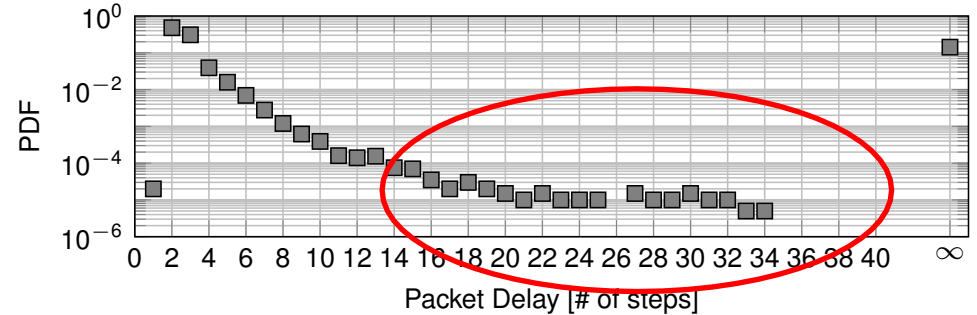
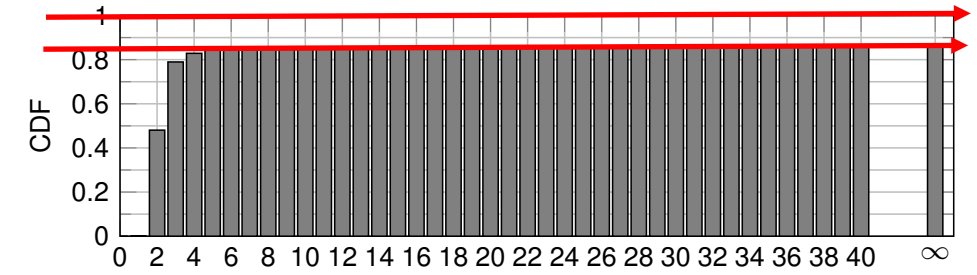


# Wi-Fi in the loop: experimental data (1kHz packets/s)

**15% loss**



**Burst losses**

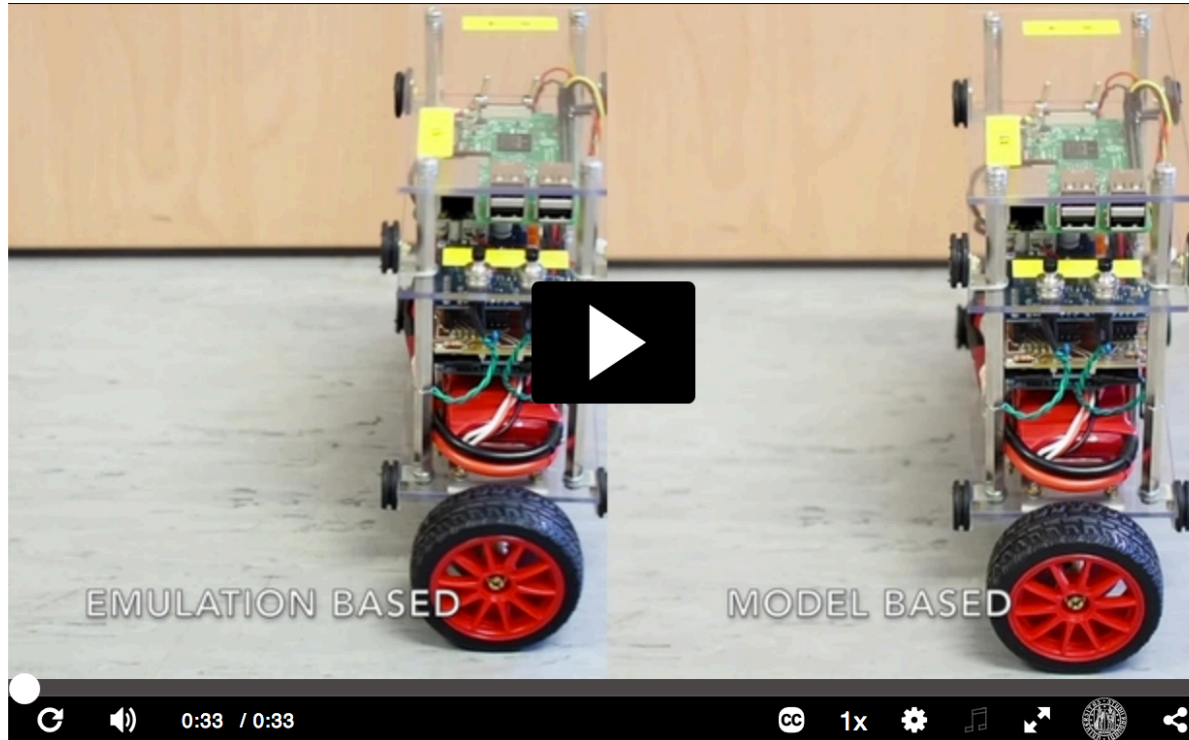


**Heavy-tail distribution**

Packet losses/delays are  
not i.i.d. nor Markovian !!



# Experimental results



MAG2IC\_Drive-By-WiFi

▶ 7 ◉ 0

[https://mediaspace.unipd.it/channel/MAG2IC\\_channel/182529591](https://mediaspace.unipd.it/channel/MAG2IC_channel/182529591)

F. Branz, R. Antonello, M. Pezzutto, F. Tramarin, S. Vitturi, L. Schenato. Drive-by-Wi-Fi: Model-Based Control over Wireless at 1-kHz. *IEEE Transactions on Control Systems Technology* [conditionally accepted], 20XX



# Future direction: Safe "control" over wireless:



Matthias Pezzutto

Ph.D. student  
Univ. of Padova



Emanuele Garone

Reference Governor  
ULC, Belgium



Ruggero Carli

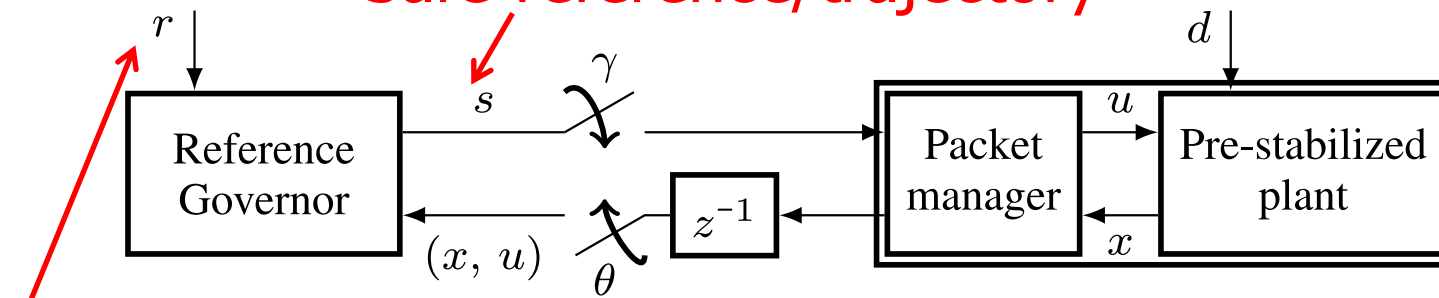
Networked Control  
Univ. of Padova



Marcello Farina

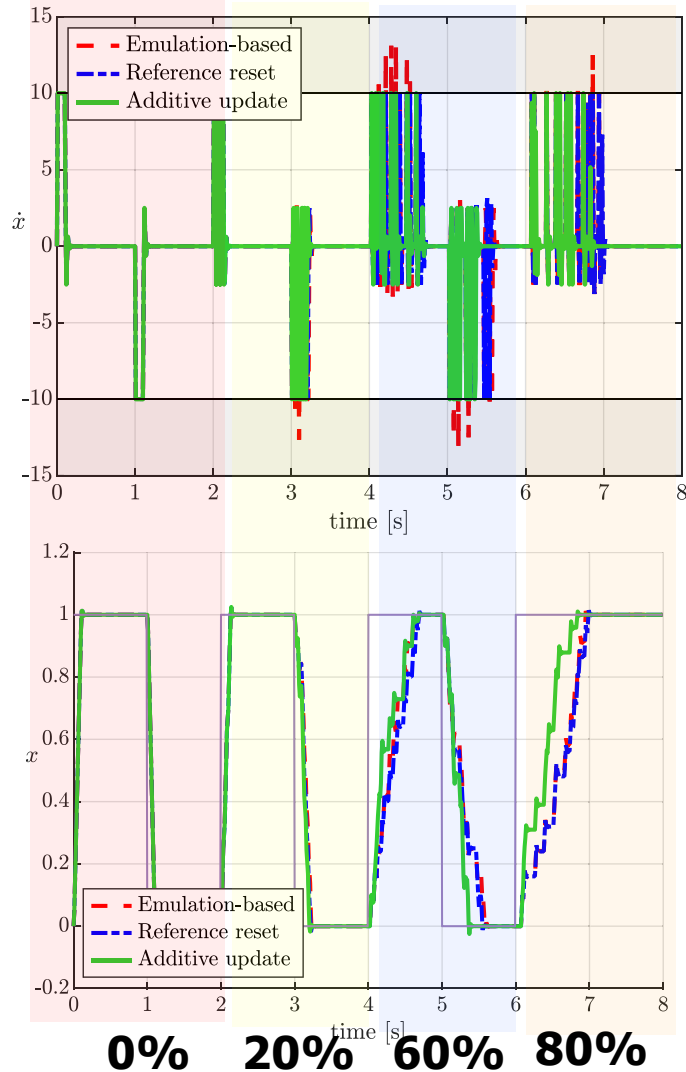
MPC  
Polytech. of Milan

Safe reference/trajectory



True Reference/Trajectory to be followed

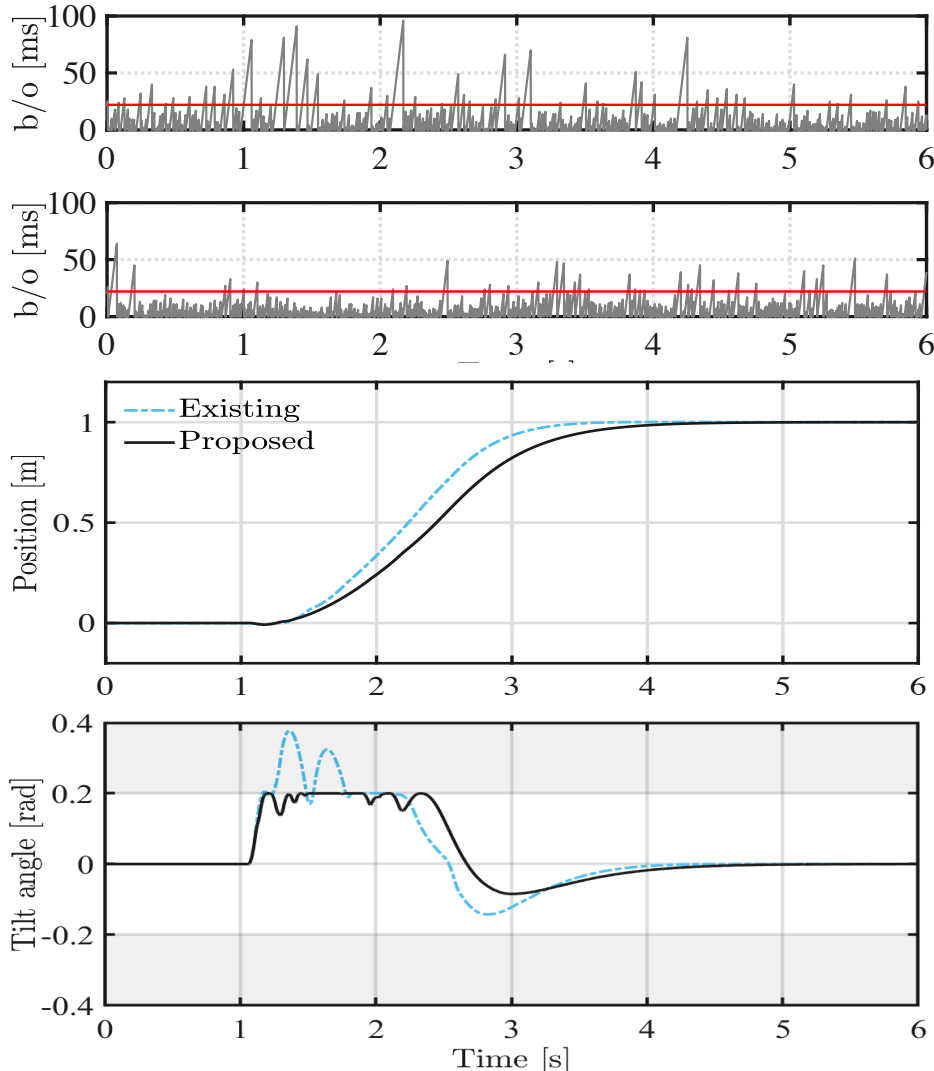
# Safe "control" over wireless: reference governor approach



- **Constraints always satisfied** even in absence of communication
  - Safe to communication blackout
  - Predictive packetized control
- Suitable for non i.i.d. time-varying channels
- **Performance adapts** to quality of channel



# Safe "control" over wireless: MPC approach



- **Constraints always satisfied** even in absence of communication
  - Safe to communication blackout
  - Predictive packetized control
- Implemented using experimental Wi-Fi in the loop
- **Performance adapts** to quality of channel



# Conclusions & open problems

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- Need to look at realistic assumptions (in particular communication)
- WI-Fi is suitable for 1kHz applications and 5G is coming: needs more experimental work.
- Move from Stability to Safety in Control Over Wireless
- Cooperation over Wireless for multi-agent systems: pristine area



# Questions ?

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Papers available on personal homepage:

URL: <http://automatica.dei.unipd.it/people/schenato.html>